

Using Auxiliary Population Samples for Sample-Selection Correction in Models Based on Crowd-sourced Volunteered Geographic Information

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ABSTRACT

Citizen science (CS) projects offer a selected sample with extensive information about human interactions with the natural world. We independently survey (1) members of the eBird CS project and (2) a general population sample, eliciting awareness and/or levels of engagement with the eBird project in each case. The general-population sample yields an ordered-probit model to explain propensities to engage with eBird, which we transfer to predict selection-correction terms for our separate sample of eBird members. We illustrate, using a spatial extent-of-the-market model for birding excursions based on a question posed only to our eBird member survey sample.

1 Introduction

“Citizen science” or “community science” (CS) projects recruit volunteers from the general population to help scientists gather data about the natural world. For many CS projects, mobile apps or web portals enable people to store their observations, and to include volunteered geographical information (VGI), either automatically or on a discretionary basis, as they contribute to the project.¹ In the context of ordinary market goods, of course, numerous private companies worldwide collect and process vast quantities of human geographic mobility data to track consumer behavior for market research. CS VGI data, likewise, constitute a vast amount of very granular individual-level data about people’s interactions with non-market environmental goods. These data pertain only to the contributing set of citizen scientists, but with careful attention to selection corrections, they represent a potentially valuable research resource for environmental economists.

For environmental economics research, one valuable CS/VGI data source is related to bird-watching. About 45.1 million Americans observed birds, both around home and away from home, according to the 2016 Survey of Fishing, Hunting and Wildlife-Associated Recreation.² The eBird project, managed by the Cornell Lab of Ornithology, is the world’s largest biodiversity-related CS undertaking. For 2019, eBird reports over 500,000 members collecting 737 million bird observations.³ Worldwide, in that same year, users of eBird’s mobile app contributed more than 6.2 million eBird checklists (reports) of bird observations. Published

¹CS projects have proliferated because of the growing ability of participants to contribute real-time field observations using convenient smart-phone applications. As of February 2020, there are now more than 2,000 active CS projects, according to the *Citizen Science Association* (see CitizenScience.Org), 448 are registered in the federal crowd-sourcing and CS registry (see CitizenScience.Gov/Catalog/#).

²Our own general-population survey asks about a wide variety of interactions with wild birds, including “pause what you are doing to observe wild birds.” Fully 88% of our sample reports doing this at least once over the past year, suggesting that incidental interest in wild birds extends beyond just those people who consider themselves to be bird-watchers. About 67% of our sample reports traveling more than one mile to see birds on at least one occasion during the past year, yet less than 12% report being active or inactive members of the eBird CS project. In Online Appendix A, Table A1 summarizes levels of activities related to wild birds.

³This 2019 eBird review is available online at <https://ebird.org/news/ebird-2019-year-in-review>.

examples of the use of eBird CS/VGI data to value environmental goods (specifically, avian biodiversity) include Kolstoe and Cameron (2017), Roberts et al. (2017) and Kolstoe et al. (2018). Beyond these studies using eBird data, other research concerning visitation patterns and the demand for non-market environmental goods have employed, for example, data from social media platforms such as Flickr.⁴

The observation and enjoyment of wild birds is a popular recreational pursuit that previously left little in the way of a “data footprint” compared to other recreational activities (such as those which require permits, licenses, or entrance fees). CS projects such as eBird, however, provide a wealth of observations about human interactions with environmental public goods because they assemble vast quantities of data on the activities of project participants over time.

The widespread spatial and temporal availability of ecosystem-related CS data like eBird make these data potentially very useful for studies of how ecological changes affect non-market or recreational ecosystems services enjoyed by humans. For example, CS data have been used to document the fact that degradation of the ecosystems that serve as wild bird habitat has adversely affected wild bird populations. Rosenberg et al. (2019) report an estimated net loss of about three billion birds since 1970—a 29% net loss in roughly five decades. Climate change, urbanization, and changes in land cover in coming decades are likely to cause even more losses, as well as changes in the geographical ranges of individual bird species. Efforts to monitor ongoing changes in wild bird populations, and to better understand the “human dimensions of wildlife” in this context, require data on both (a) these bird populations themselves and (b) the preferences of the human population regarding alternative policies with respect to wild birds. Both types of information are essential to any

⁴Wood et al. (2013) first pointed to online social media applications as a possible source of “big data” concerning nature-based tourism and recreation. Visitation studies, such as those done by Wood et al. (2013), Sessions et al. (2016), and Sonter et al. (2016) employ Flickr data. A non-market valuation study using the Flickr data is described in Keeler et al. (2015), who estimate the recreational demand for clean water.

benefit-cost analyses of alternative policies to protect or enhance populations of wild birds as natural assets.

Unfortunately, groups of citizen scientists are not likely to be representative of the general population. Rather than being random samples, these groups must be classified as “samples of convenience.”⁵ Of course, non-representative voluntary surveys are often used to collect data, and a variety of different methods have been developed to correct for respondents’ differing propensities to respond to the survey and therefore to be part of the estimating sample (either via the traditional method of Heckman (1979), a foundational paper for the least-squares context, now cited more than 10,000 times in Web of Science, or via alternative ad hoc approaches as in Cameron and DeShazo (2013) and Johnston and Abdulrahman (2017)). For data collected from CS participants, self-selection bias may arise from the potential correlation between the unobserved components of (a) their propensities to engage with the CS project to different degrees, and (b) their outcome variable of interest concerning the environmental good being studied in a CS sample.

In this paper, we address systematic sample selection that must be considered, when harnessing CS/VGI data, to make any potential inferences based on these samples more useful for policy-makers. We use, in tandem, a survey of eBird members in the Pacific Northwest and a completely independent representative nationally sample from a survey of the general population of the U.S. Both of our samples include information from respondents about the extent to which they participate in the eBird project, so that we can distinguish not only the extensive margin (whether an individual participates in eBird), but how intensively they engage with this CS project.

We propose three candidate strategies. At the most basic level, we use our two samples to construct estimated heterogeneous sampling weights that permit corrections for different

⁵Convenience samples can still be immensely valuable if the research object is merely to establish that a relationship among variables *can* exist, but they do not permit the researcher to generalize statistical results from the sample to the overall population.

relative frequencies of engagement with eBird (at different levels of intensity and for different types of people) across our general population survey and our survey of eBird members.

Our second strategy, which is a more-structural approach, is to develop “inverse Mills ratio *functions*” that can be estimated using the general population sample and transferred to the eBird member survey sample. This approach relies upon strong assumptions about joint densities and allows only the expected value of the outcome variable to be distorted by sample selection bias.

A third approach is to transfer “engagement propensity *functions*” from the general population sample to the eBird member survey sample (as a more ad hoc correction approach). Deviations of individual predicted engagement propensities (in the eBird member survey sample) from the sample mean in the qBus general population sample can be allowed to shift the estimated parameters in the outcome equation of interest. This allows both the intercept and the slopes of the outcome equation to be biased by systematic sample selection, albeit less elegantly.

To illustrate our correction methods, we tackle a persistent methodological issue that plagues the empirical non-market valuation of environmental goods, as well as scaling-up tasks or benefit-transfer exercises employing these values. Specifically, we directly address the question of the relevant spatial market extent for individual demands (e.g. Loomis (1996), Walsh et al. (2011)). This issue is also described as “distance-decay” in willingness to pay (e.g. Johnston et al. (2019)) or spatial preference heterogeneity (e.g. De Valck and Rolfe (2017), Logar and Brouwer (2018), or Badura et al. (2020)). Spatial market extents are likewise intimately related to the notion of consideration sets for models of destination choice (e.g. von Haefen (2008)).⁶

Since at least Smith (1993), researchers have expressed concerns about the issue of het-

⁶Outside environmental economics, the concept of market extent is also relevant in the marketing literature (e.g. Jank and Kannan (2005) and the transportation geography literature (e.g. (Rodrigue et al., 2016, pg. 346)).

erogeneous preferences and the geographic extent of the market. In scaling sample estimates to the implied aggregate benefits, assumptions about the extent of the market may sometimes be even more important than any sensitivity in the estimates of individual values. Bateman et al. (2006) warn of the perils of aggregating individual benefits estimates over political jurisdictions, rather than the relevant extent of the market. Newbold et al. (2018) identify the geographic extent of the market in households' WTP for environmental goods as an important challenge in benefit transfer for active use values of natural assets.

To permit this illustration, we included in our eBird member survey a specific question about each respondent's personal geographical "extent of the market" for typical one-day birding excursions. The birding destinations within the respondent's personal market extent can be interpreted as the relevant "consideration set" for their destination choices. Most previous research concerning recreational destination choices (e.g. Dundas and von Haefen (2020)) has tended to use a common market extent for all individuals, often choosing a distance that has been used in other studies concerning similar environmental goods. Sometimes an assumption about a single common market extent is loosely informed by the upper percentiles of the observed marginal distribution of distances actually travelled across all trips in the data, as in Kolstoe and Cameron (2017). Other recent research has grid-searched across possible market extents and employed the single market extent for all individuals that maximizes the model likelihood (Holland and Johnston, 2017). Here, we seek to identify systematic variations across our sample of eBird members in their directly elicited individual market extents. Our fitted market extent *function* may then be transferable to other samples of birders from the general population, but only if the results are corrected for self-selection bias in our sample of eBird citizen scientists.

In Section 2 of this paper, we review a few examples of efforts at sample selection correction in the environmental economics literature. Section 3, as a preamble, revisits the conventional intuition for two-step sample selection corrections with a binary-probit selec-

tion equation. We then explain how to use a selection equation, estimated for one sample, to construct an inverse Mills ratio function that can then be transferred to an independent sample, and follow up with a generalization of this approach from binary probit to a six-level ordered-probit selection equation. We also describe an ad hoc alternative correction method, where the correction is not derived formally to imply the use of an inverse Mills ratio. For good measure, for our analysis of individual market extents, we develop heterogeneous sampling weights based on ordered-probit models for eBird engagement intensity fitted separately to the general-population sample and the eBird member survey sample, but we relegate the details of our weighting strategy to an online appendix. Section 4 discusses our estimated selection models, and Section 5 discusses our “outcome” model for heterogeneous spatial market extents for birding excursions. We compare parameter estimates and predicted market extents when the model is estimated both naively and with our different types of selection correction strategies. Section 6 concludes and provides some recommendations for future general-population data collection.

2 Sample-Selection Bias and Correction in the Related Literature

Overcoming the problem of CS samples of human participants being “samples of convenience” requires addressing the sample-selection problem. To date, the literature has focused mostly on strategies to correct for survey “unit” non-responses, or the effects of additional exclusion restrictions based on “item” non-response for key variables. Sample selection correction methods are familiar in the case of continuous outcome variables, as reviewed by Vella (1998) and Wooldridge (2002). But sample-selection correction methods for multiple discrete out-

comes are not particularly well developed in the environmental literature.⁷ For conditional logit discrete-choice outcome models, Johnston and Abdulrahman (2017) use an ad hoc approach that builds on earlier work by Cameron and DeShazo (2013) to adjust for response propensity. Kolstoe and Cameron (2017) and Kolstoe et al. (2018) also use this approach, but employ the method to correct only for the individual’s propensity to be in the estimating sample drawn from the population of eBird members, not the propensity to be an eBird member in the first place (see the Online Appendix from Kolstoe and Cameron (2017) for details).

Yuan et al. (2015) use a binary probit model to explain systematic selection into their estimating sample and compute an inverse Mills ratio (IMR). This IMR is used as a regressor in their second-stage conditional logit choice model, to shift the coefficient on the status-quo alternative in their choice sets.⁸ However, a simple IMR term is appropriate only when the selection propensity and the (possibly transformed) outcome variable of interest are jointly normally distributed. The Heckman logic for using an IMR thus does not apply when the outcome model is a conditional logit specification—one cannot appeal to the usual bivariate normality assumption for the errors in the two equations to argue that the inclusion of this IMR variable in the outcome equation precisely solves the problem of selection bias. Given that the bivariate normality assumption is untenable in this case, there is no good argument for converting the selection propensity into an IMR term.

⁷Terza (2009) proposes a strategy for multinomial (multi-index) models, but does not illustrate his approach for the conditional logit models relevant to destination choice models or stated-preference choice experiments common in the environmental literature.

⁸Given that the IMR derived from the selection model is individual-specific but does not vary across alternatives, including it in the utility-difference “index” that underpins a conditional logit model requires that the IMR term be interacted with at least one regressor that actually *does* vary across alternatives. A status-quo indicator is one such variable.

3 Strategies for Dealing with Systematic Sample Selection in eBird data

Our “eBird member survey” sample is self-selected, consisting only of eBird members who chose to respond to our survey. These birders are also likely to participate in the eBird project with a different mix of engagement levels than might be expected for members of the general population who participate in birding. For this study, over several waves of the Qualtrics Omnibus (qBus) survey, we independently surveyed more than 4000 respondents from that survey research firm’s general-population panel. In Online Appendix A, Table A2 contrasts our simple binary indicator for eBird citizen-science participation, CS , with the greater detail in our six ordered categories of engagement intensity, $CS6$, elicited in both the qBus data and in our sample of eBird members.⁹

3.1 Review standard intuition based on binary selection

In framing the *intuition* for our models, we will start by aggregating our six possible engagement levels into just two: non-eBird members in the general population, and eBird members in the general population. This allows us to develop our approach, initially, in terms of a more-familiar binary indicator for “selection into citizen science project participation,” where eBird is the specific citizen science project in this example. Let CS_i be 1 if the respondent is a member of eBird (reporting bird sightings at any frequency) and 0 if the respondent is not a member of eBird (regardless of whether they have heard of the eBird project).¹⁰

⁹The Qualtrics Omnibus surveys have been discontinued, but there remains the equivalent (if somewhat more expensive) option of using the regular Qualtrics panel for a very short regular survey. Alternatively, any other general-population consumer panel could be used.

¹⁰We will assume, in this proof-of-concept example, that respondents to the qBus questions are essentially a representative sample of the general population, and respondents to the analogous questions posed to our eBird member survey are essentially a representative sample of eBird members. Unlike our previous research with eBird data, the current analysis is not affected by substantial shares of missing or out-of-date home address information needed to allow calculation of actual travel distances from each person’s home to all of their relevant birding destinations.

3.1.1 Binary selection and the general population sample

For the $i = 1, \dots, N$ individuals in our general population (qBus) sample, we have observations for some people who are members of eBird and other observations for other people who are not. For everyone, we have conformable variables on sociodemographics and income, Z_i , that we will use to explain eBird participation or non-participation, where respondents $i = 1, \dots, r$ participate in eBird and respondents $i = s, \dots, N$ do not:

$$CS_i = \begin{bmatrix} 1 \\ \vdots \\ 1 \\ 0 \\ \vdots \\ 0 \end{bmatrix}, Z_i = \begin{bmatrix} Z_{11} & \dots & Z_{k1} \\ \vdots & & \vdots \\ Z_{1r} & \dots & Z_{kr} \\ Z_{1s} & \dots & Z_{ks} \\ \vdots & & \vdots \\ Z_{1N} & \dots & Z_{kN} \end{bmatrix}$$

For the qBus sample, we will model the latent propensity to be a member of eBird as $CS_i^* = Z_i\gamma + \eta_i$. Given only these data for the qBus sample, we cannot estimate a second model to explain the outcome variable of interest, $y_i = X_i\beta + \epsilon$, because there are no data for our y_i variable of interest in the qBus sample. (That variable is collected only in our separate eBird member survey sample.)

One might wonder whether a researcher could simply pose all the questions on our eBird member survey to a large sample of respondents from the general population. Such a survey would be possible, if we were interested only in the illustrative outcome variable explored in this study. However, such a survey could not take advantage of the wealth of other “passive” birding participation data also available for eBird members. While we might have replicated our eBird member survey with the qBus general population sample, this would have been much more expensive than adding just a couple of key questions to the regular qBus survey. Just fielding our eBird member survey to a special-purpose Qualtrics sample would not permit responses to be linked to the associated eBird profiles and detailed birding histories available for eBird members. Identity protections in the Qualtrics panel preclude

us from being able simply to ask any eBird members in the qBus sample for their name or eBird member number (if the respondent even knows their member number).

Hypothetically, however, *if* we could somehow collect from each eBird member who turned up in our qBus sample responses to all of the questions we asked in our separate survey of eBird members, we could use the standard selection correction approach and specify both the selection equation and the equation to explain some outcome variable of interest, y , using the qBus data alone, as:

$$\begin{aligned}
 CS_i^* &= Z_i\gamma + \eta_i & (1) \\
 y_i &= X_i\beta + \epsilon_i \\
 (\eta_i, \epsilon_i) &\sim BVN(0, 0, \sigma_\eta, \sigma_\epsilon, \rho)
 \end{aligned}$$

where the subscript i will be used to denote observations from the qBus sample. This would be the standard sample selection story.

3.1.2 Binary selection and the eBird CS sample

In contrast, for the $j = 1, \dots, J$ observations from our eBird member survey sample, we have Z_j variables that conform to the Z_i variables in the qBus sample, but we have no information about anyone for whom $CS_j = 0$ (i.e. everyone in this sample is a member of eBird). In this case, the selection process cannot be modeled using the eBird data alone because there is no variation in the selection outcome for this group. However, we have data on an outcome variable of interest for this sample, y_j (in this case, the individual’s “market extent”, namely their maximum one-way distance for a one-day birding trip), and regressors, X_j , to explain this outcome, where this information is not available for the qBus sample:

$$CS_j = \begin{bmatrix} 1 \\ \vdots \\ 1 \end{bmatrix}, Z_j = \begin{bmatrix} Z_{11} & \dots & Z_{k1} \\ \vdots & & \vdots \\ Z_{1J} & \dots & Z_{kJ} \end{bmatrix}, y_j = \begin{bmatrix} y_1 \\ \vdots \\ y_J \end{bmatrix}, X_j = \begin{bmatrix} X_{11} & \dots & X_{m1} \\ \vdots & & \vdots \\ Z_{1J} & \dots & Z_{mJ} \end{bmatrix}$$

For our eBird member survey sample, we will assume that the underlying relationship between CS and the Z variables is identical to the analogous relationship in the qBus sample. Our proposed selection-correction method will be appropriate if the identical γ and β parameters *would* apply in this eBird sample (and the same $\sigma_\eta, \sigma_\epsilon, \rho$, as well). If the selection equation *could* be estimated for the $j = 1, \dots, J$ observations in the eBird member survey sample, the relevant pair of equations would be:

$$\begin{aligned} CS_j^* &= Z_j\gamma + \eta_j \\ y_j &= X_j\beta + \epsilon_j \\ (\eta_j, \epsilon_j) &\sim BVN(0, 0, \sigma_\eta, \sigma_\epsilon, \rho) \end{aligned} \tag{2}$$

Of course, this joint model cannot be estimated because the observed CS_j variable is constant (at 1) in the data from our eBird member survey.¹¹

3.1.3 Transferring a fitted selection equation

The challenge is that we do not have y_i and the X_i variables for the eBird members in the qBus general population sample. Instead, we have these variables only for our completely separate sample of eBird members. If we can assume that participation in eBird in the general-population qBus sample follows the same data-generating process as the one that determines participation in eBird among people in our eBird member survey sample, we can assume likewise that $(CS_j^*, y_j) \sim BVN(Z_j\gamma, X_j\beta, 1, \sigma_\epsilon, \rho)$ for $j = 1, \dots, J$ for members of

¹¹For readers who may wish to review the conventional Heckman two-step sample-selection correction procedure in more detail, we provide a summary in Online Appendix B.

our eBird sample.¹²

The crux of this approach is that we transfer the $\hat{\gamma}^q$ estimates from the qBus sample to construct a fitted index, $Z_j\hat{\gamma}^q$, to predict the selection process for the eBird sample, even though we have no data from non-eBird members in the eBird member survey sample. The conditional expected value and variance for y_j will be calculated as follows, noting the j subscripts for the eBird data.¹³

$$\begin{aligned} E[y_j|y_j \text{ observed}] &= E[y_j|CS_j^* > -Z_j\hat{\gamma}^q] = X_j\beta + \rho\sigma_\epsilon\lambda(-Z_j\hat{\gamma}^q) \\ &= X_j\beta + \beta_\lambda\lambda(-Z_j\hat{\gamma}^q) \end{aligned} \quad (3)$$

$$Var[y_j|y_j \text{ observed}] = Var[y_j|CS_j^* > -Z_j\hat{\gamma}^q] = \sigma_y^2 [(1 - \rho^2)\delta(-Z_j\hat{\gamma}^q)]$$

The inverse Mills ratio, $\lambda(-Z_j\hat{\gamma}^q)$ is equal to $\phi(-Z_j\hat{\gamma}^q)/(1 - \Phi(-Z_j\hat{\gamma}^q)) = \phi(Z_j\hat{\gamma}^q)/\Phi(Z_j\hat{\gamma}^q)$, where $\phi(\cdot)$ is the standard normal probability density function (pdf) and $\Phi(\cdot)$ is the corresponding cumulative density function (cdf). The desired unconditional (i.e. non-systematically selected) expectation for y_j can be simulated, counterfactually, by setting $\rho = 0$, so that $E[y_j] = X_j\beta$.

¹²Mechanically, it would be possible to pool our two samples and use the combined dataset to estimate one common selection equation. The advantage of using the qBus sample, alone, for the selection equation is that the qBus data represent a random sample from the general population. Pooling it with the eBird sample, however, produces a dataset that no longer represents the general population. One could, potentially, weight the eBird member survey sample according to the proportion of eBird members in the qBus sample, but this would still leave a pooled sample for the selection equation that is not randomly selected from the general population.

¹³We note that it is not uncommon for samples to have error distributions with different scales. Probit (and ordered-probit) models normalize their parameters on the error standard deviation for the model, so the estimated coefficients in the selection models we estimate using the qBus data are known only up to a scale factor. Each γ coefficient is implicitly γ^*/σ_η , where the σ_η applies to the qBus data. If the value of σ_η is larger or smaller for the eBird sample, employing the coefficients estimated on the qBus sample would lead to predicted engagement intensities in the eBird sample that are biased proportionately downward or upward, respectively. Joint estimation using the two samples is feasible in principle, but prohibitively difficult in the current case because of the strategy we use to deal with missing variable values, discussed later in this paper. Here, therefore, we assume the qBus and eBird selection-equation error distributions are identical.

3.2 Generalizing to a six-level ordered-probit selection model

We now change the model to acknowledge that participation or engagement in eBird is more complex than just a simple yes/no indicator (i.e. an “extensive margin” decision). A standard selection model will not take advantage of the extra information we have about people’s various different levels of engagement with eBird. Our qBus questions elicit six levels of eBird engagement intensity, and our eBird member survey questions elicit four corresponding levels of eBird engagement intensity, conditional (obviously) on at least some level of participation in eBird. This additional level of detail provides unusual but valuable information about the “intensive margin” of participation in eBird, for both of our samples.

We now show how standard two-stage sample selection correction methods can be adapted to accommodate an ordered categorical selection variable with six levels (based on an analogous latent continuous “propensity to engage” with the eBird citizen science project). Compared to the standard binary selection equation reviewed in Section 3.1, our generalization is built around a six-level ordered-probit model for the qBus general population sample and a four-level ordered-probit model for the eBird member survey.¹⁴

We will assume that the joint distribution of the error terms in the underlying (latent continuous) $CS6_i^*$ and y_i variables can be assumed still to be jointly normal, so that the formulas for the moments of a singly-truncated bivariate normal distribution still apply. Then the calculated IMR selectivity-correction term based on the adjusted $\hat{\gamma}^q$ ordered-probit estimates from the qBus sample and the Z_j variables from the eBird sample can still be

¹⁴An adjustment may be necessary, to the intercept of the fitted propensity-to-engage with eBird, depending upon which software is used to estimate the ordered probit model. Comparability is necessary if one wishes to compare fitted “propensity” estimates from this ordered-probit selection model to those produced when a standard binary-probit model is used in first step of a typical two-step correction model. In Stata, for example, the *intercept* of the “index”, $Z_i\gamma$, is normalized to zero and five distinct “cuts” (thresholds of the latent continuous propensity variable CS_i variable) are estimated. More generally, if there are K levels of an ordered probit model, Stata estimates K-1 “cuts” in the latent continuous propensity variable. To produce fitted propensity estimates that are comparable across the binary probit and ordered-probit versions of the selection equation, it is necessary normalize to zero not the *intercept* in the ordered probit model, but the “cut” between the second and third categories in the six-level ordered probit selection model.

calculated as $\phi(Z_j\hat{\gamma}^q)/\Phi(Z_j\hat{\gamma}^q)$. As in the case of a binary probit selection correction, this term can be appended to the list of regressors, X_j , in the outcome equation of interest.^{15,16}

3.3 Ad hoc alternative: Interactions with demeaned propensities

In lieu of a formally derived Heckman-type selection-correction model, an ad hoc approach can be entertained. We use the estimated engagement propensity model from our first-stage selection model to calculate fitted propensities to engage with eBird at each of six levels (in the qBus sample) or predicted propensities to engage with eBird at four levels (in the eBird member survey sample). For any individual in the eBird member survey sample with a given set of X_j variables, their “predicted engagement propensity” can then be used just like any other type of individual-specific heterogeneity, such as indicators for gender, age, employment status, or educational attainment.

In a true random sample from the general population, every individual in the population is equally likely to show up on the sample. Self-selected samples of CS participants are not expected to be representative of the the general population. If we treat our qBus sample as representative of the general population, the predicted engagement intensities for our eBird member survey sample can be demeaned relative to the average engagement propensity for the general-population qBus sample. This fitted demeaned engagement propensity variable can then be allowed to shift all of the key parameters in the outcome model of interest. After estimation of the outcome model, this demeaned response propensity can be counterfactually

¹⁵It will be appropriate, in future research, to graduate to a full-information maximum likelihood joint estimation of the selection equation and the outcome equation. The ordered-probit form for the selection model is atypical, so no packaged algorithms exist to permit FIML estimation of a “selection-on-ordered-probit” model. We note that there is a packaged algorithm for “ordered probit models with selection,” but this is not what we need. That model has a conventional binary-probit selection model and an outcome equation that should be estimated as an ordered-probit model.

¹⁶In Online Appendix C, we provide a detailed discussion of the types of outcome models where may be appropriate to contemplate just adding an IMR term to correct for sample selection. Here, we simply note that this straightforward strategy may be suitable only if the latent continuous dependent variable selection equation and the observed (or latent) continuous dependent variable in the outcome equation can be modeled as involving error terms that are plausibly jointly normally distributed.

set to zero, effectively dropping all of the interaction terms in which it is involved. The resulting outcome equation, without these interaction terms, then applies (in principle) to the case where everyone in the estimating sample shares an engagement propensity equal to the average engagement propensity in the general population qBus data—namely, for a “representative” sample.

Ideally, one or more exogenous explanatory variables should be *included* in the $Z_i\gamma$ index that yields the fitted engagement propensities, but *excluded* from the $X_j\beta$ index that represents the conditional expected value of the outcome variable of interest. This is analogous to the need for “omitted exogenous variables” (i.e. instruments) in two-stage least squares estimation. Suppose there are too few variables in the selection model that do *not* also appear in the outcome equation. Then the fitted engagement propensity can be very close to a linear combination of the other variables used to explain the outcome variable of interest. The resulting multicollinearity problem can inflate the standard errors on the coefficient(s) of interest in the outcome equation and/or render those estimates insufficiently robust to minor differences in the specification of the joint model.¹⁷

4 Selection Model: Implementation

4.1 Available variables for selection model

Our selection equations, either binary probit or ordered probit, require conformable measures of the Z_i and Z_j variables (i.e. these variables must be measured in the same way for the qBus and eBird member survey datasets). For the qBus data, unless one wishes to pay for additional questions, it is necessary to make do with the default set of sociodemographic and geographic characteristics that are available for all qBus panelists, as collected

¹⁷In two-step selection-correction models, of course, the non-linear transformation used to create the inverse Mills ratio variable breaks this exact collinearity, but it is considered poor form to attempt to identify the second-step parameters solely on the basis of this non-linear transformation.

by Qualtrics. Thus we aggregate both the qBus and the eBird member survey Z variables to the same level, yielding conformable sets of indicator variables for the different levels of each of seven individual characteristics that can be allowed to influence either engagement or non-engagement in the eBird CS project (in the binary selection model) or the different intensities of engagement (in the more-general ordered-probit selection model).

The available variables for our selection model, conformably aggregated, are as follows:

- Annual number of birding excursions of more than one mile away from home (12 bins)
- Whether the individual has participated in the Audubon Christmas Bird Count (0/1)
- Whether the individual also hunts birds (0/1)
- Gender = female (0/1)
- Age (6 brackets)
- Race (4 groups)
- Ethnicity (2 groups)
- Income (5 brackets)
- Geography (4 regions)
- Employment status (5 categories)
- Educational attainment (5 levels)

Across observations with no missing values, for the qBus data ($N=4,161$) and for the eBird member survey data ($J=1,081$), Table 1 summarizes the proportions of observations in each set of indicator variables. Note that respondents in the qBus sample have two more options than respondents in the eBird member survey sample. The qBus respondents can also choose the engagement categories “Unfamiliar with eBird CS project” or “Heard of eBird but not a member.” As a consequence, it is not possible to compare directly the proportions in the other four eBird-member engagement-intensity categories across the qBus and eBird samples. If we calculate the qBus conditional distribution solely for engagement

levels 3 through 6 (where a qBus respondent is at least a member of eBird), then the pairs (proportion qBus, proportion eBird) for these four engagement intensities are (0.273, 0.398), (0.252, 0.275), (0.265, 0.179), and (0.210, 0.146). While these relative proportions differ, it is also possible that the *types* of people who respond to the qBus survey may differ from the *types* of people who are enrolled in eBird and responded to our survey of a random sample from only the eBird population.

As detailed in Table 1, there are a number of notable differences between our two samples. For the annual number of days with trips of more than one mile to observe birds, we defined bins roughly according to deciles of the qBus distribution between 1 and 364 days. Only 44% of the qBus sample responds to this question, but we can construct this variable for 77% of the eBird sample.¹⁸ Our eBird respondents are less likely to have taken zero such trips, and more likely to claim to have traveled to see birds all 365 days of the year.

Our eBird member survey respondents are more likely to have participated in the Audubon Christmas Bird Count, and they are much less likely to hunt birds. They are somewhat more likely to be female and to be older.¹⁹ A considerably larger share of the eBird member survey sample did not provide any income data (29.6 percent). Everyone in the eBird member survey sample is from the states of Washington and Oregon, whereas the qBus sample is nationwide. Compared to qBus respondents, more than twice as many eBird member survey respondents are retired. Finally, the eBird member survey sample reports higher educational attainment. All of these differences point to empirical evidence of systematic selection on observables, so that selection on unobservable factors is also likely to be a concern.

¹⁸To construct an analogous distribution for our eBird sample, we combine their actual number of days with submitted birding checklists over the preceding twelve months with their self-report as to what fraction of their bird sightings they report to eBird. The documented information about their actual trips distinguishes this constructed explanatory variable from the engagement intensities that form the outcome variable.

¹⁹They are also more likely to identify as White. However, the proportions of Black and Asian and Hispanic eBird respondents are all less than 1 percent, so we will not use the Race or Ethnicity indicators in our specifications.

Table 1: Descriptive statistics (proportions) for first-stage Bird engagement intensity Availability indicators are proportions of total sample; group shares are proportions of available data

	qBus proportions	eBird proportions
Engagement data available	1.000	1.000
1=Unfamiliar with eBird CS project	0.802	0.000
2=Heard of eBird but not a member	0.083	0.000
3=eBird member, but report rarely	0.031	0.391
4=eBird member, report < 1/2 of birds	0.029	0.280
5=eBird member, report > 1/2 of birds	0.030	0.177
6=eBird member, report almost all birds	0.024	0.152
Travel 1+ mile data available	0.442	0.769
Trips 1+ miles = 0	0.348	0.277
Trips 1+ miles = [1,4)	0.063	0.113
Trips 1+ miles = [4,7)	0.065	0.065
Trips 1+ miles = [7,10)	0.048	0.025
Trips 1+ miles = [10,21)	0.076	0.093
Trips 1+ miles = [21,41)	0.065	0.065
Trips 1+ miles = [41,72)	0.063	0.078
Trips 1+ miles = [72,124)	0.065	0.067
Trips 1+ miles = [124,174)	0.063	0.052
Trips 1+ miles = [174,238)	0.063	0.032
Trips 1+ miles = [238,364)	0.062	0.054
Trips 1+ miles = 365	0.017	0.078
Audubon CBC data available	1.000	1.000
Has participated in CBC	0.092	0.528
Bird hunting data available	1.000	1.000
Hunts birds	0.224	0.073
Gender data available	1.000	0.994
Gender: Male	0.489	0.427
Gender: Female	0.511	0.573
Age data available	1.000	0.993
Age: 24 years or less	0.125	0.018
Age: 25 to 34 years	0.224	0.065
Age: 35 to 44 years	0.196	0.089
Age: 45 to 54 years	0.135	0.146
Age: 55 to 64 years	0.175	0.311
Age: 65 years and up	0.145	0.370
Income data available	1.000	0.804
Income: Less than 25K	0.179	0.072
Income: 25 K to 50 K	0.219	0.203
Income: 50 K to 75 K	0.189	0.231
Income: 75 K to 100 K	0.141	0.173
Income: 100 K or more	0.272	0.321
Region data available	1.000	1.000
Region: West	0.225	1.000
Region: Northeast	0.186	0.000
Region: Midwest	0.217	0.000

Region: South	0.372	0.000
Empl. status data available	1.000	0.849
Empl. status: Full time	0.473	0.359
Empl. status: Part time	0.132	0.080
Empl. status: Looking for work	0.057	0.008
Empl. status: Unemployed	0.145	0.066
Empl. status: Retired	0.193	0.487
Education data available	1.000	0.976
Education: High school	0.226	0.036
Education: Some college	0.356	0.158
Education: College grad	0.263	0.288
Education: Masters degree	0.118	0.396
Education: Doctoral degree	0.038	0.121
Observations	4161	1081

4.2 Estimation results for selection model

4.2.1 Ordered-probit qBus propensities to engage with eBird

The qBus sample has virtually complete data for its Z_i variables (other than the annual number of days with birding trips more than one mile from home). This completeness stems from the fact that all of the standard demographic variables used in our selection model are part of the “profile” data supplied for each qBus panelist, rather than something we sought to elicit in our two qBus questions. There are considerably more missing values for the Z_j variables from our eBird member survey, since all of the sociodemographic information for that sample was collected during our survey, rather than being part of a standard profile. At least one relevant variable value is missing for 509 of the 1,081 respondents to our eBird member survey.

We seek to transfer from the qBus sample to the eBird member survey sample the richest possible specification of the ordered-probit selection model, consistent with the data available for each respondent in the eBird member survey sample. Online Appendix E explains in more detail our strategy for recruiting all available data for every eBird member when we

estimate engagement-propensity and inverse Mills ratio functions to be transferred from the qBus sample to the eBird sample. To accommodate all of the patterns of missing values encountered in our eBird member survey data, we need to estimate 30 different ordered-probit specifications using the qBus data. Online Appendix F gives estimates for these 30 different specifications.

Online Appendix G contains a second set of ten tables with results for the corresponding set of 30 different specifications of the ordered probit model, this time estimated using the variables available for each observation in the eBird member survey sample, to explain the *four* engagement levels that could be selected by our eBird respondents. These models, estimated using just the eBird member survey data, are required solely for the construction of our weights, as detailed in Online Appendix H.²⁰

To illustrate the corresponding engagement-intensity models for the two samples, Table 2 presents the most complete specification that can be estimated using either the qBus or the eBird member survey samples. The complete set of Z_j variables is available for only 572 of the 1,081 eBird member survey respondents.²¹

To predict participation intensities for respondents to our eBird member survey, we use the γ^q coefficients estimated from the qBus specification, such as the set of estimates in the first pair of columns in Table 2 (or the relevant version of the rest of the 30 models). We use these parameter estimates to calculate four predicted engagement-level probabilities, as well as predicted engagement intensities and inverse Mills ratio terms to be used for sample-selection corrections in outcome equations that rely upon only the eBird member

²⁰Recall that the default parameterization of the thresholds between intervals (e.g. in Stata) is not comparable between the six-interval qBus models and these four-interval eBird member survey models. E.g. for the qBus models, “cut5” is the threshold between engagement levels 5 and 6, whereas for the eBird member survey models, “cut3” is the corresponding threshold between these same two levels.

²¹For the other end of the spectrum of data completeness in the eBird member survey sample, Online Appendix E contains an analogous table for the largest model that can be estimated for *every* respondent in the eBird member survey sample without being limited by missing data. This model can use all 1,081 eBird member survey respondents who answered the question about our outcome variable, but must employ far fewer explanatory variables.

survey data. The second column of parameter estimates in Table 2 is estimated using the eBird member survey data alone. Again, we need these eBird ordered-probit models only to calculate fitted engagement-level probabilities within the eBird member survey sample, an ingredient in our heterogeneous sampling weights described in Online Appendix H.²²

In comparing the coefficient estimates for each sample in Table 2, we note numerous differences. These differences do not imply, however, that it is inappropriate to transfer our qBus estimates to the eBird member survey sample for use in our selection-correction procedures. The eBird member survey sample is a selected sample for these ordered-probit engagement-intensity models, just as it is for our outcome equation to explain individual subjective market extents. Our qBus model covers all six engagement level propensities, including the roughly 88% of the qBus general population sample who are not eBird members. In transferring the qBus propensity parameters to our eBird member survey sample, it is imperative to preserve the influence of the first two, non-eBird-member, engagement levels in our general-population qBus data.

Consider the signs and significance of the individual coefficient estimates in Table 2. For respondents who report having traveled at least one mile from home to see birds over the last year, the more days per year a respondent has made such a trip, the greater their propensity to engage with eBird. These effects are statistically significant only in the eBird member survey sample, however. Past participation in the Audubon Christmas Bird Count increases engagement propensity in the qBus sample, but this effect is not apparent in the eBird member survey sample. Whether or not the respondent also hunts birds has no discernible effect on eBird engagement intensity in either sample, although the point estimate is positive for the qBus sample and negative in the eBird member survey sample.

²²To construct our weights to be applied to each observation in the eBird member survey sample, we require engagement-level probabilities for our eBird sample that are (a) “expected,” i.e. predicted, based on parameter estimates transferred from the qBus sample, and (b) “observed,” i.e. fitted, based on parameter estimates directly from the eBird sample alone.

Table 2: Ordered-probit engagement-level models with maximum heterogeneity: 6-level model for qBus sample; 4-level model for the subset of 572 eBird survey respondents with complete data for same specification

	Ordered probit qBus data		Ordered probit eBird data	
Travel 1+ mile data available	0.136	(0.661)	- ^a	
Trips 1+ miles = 0	-0.870	(0.667)	-2.828***	(0.228)
Trips 1+ miles = (1,4)	-0.260	(0.678)	-3.113***	(0.268)
Trips 1+ miles = (4,7)	-0.554	(0.683)	-1.862***	(0.287)
Trips 1+ miles = (7,10)	-0.388	(0.681)	-2.243***	(0.372)
Trips 1+ miles = (10,21)	-0.0566	(0.667)	-1.820***	(0.250)
Trips 1+ miles = (21,41)	-0.0189	(0.668)	-1.496***	(0.262)
Trips 1+ miles = (41,72)	0.287	(0.665)	-1.354***	(0.254)
Trips 1+ miles = (72,124)	0.518	(0.663)	-0.711***	(0.258)
Trips 1+ miles = (124,174)	0.400	(0.663)	-0.644**	(0.293)
Trips 1+ miles = (174,238)	0.487	(0.662)	-0.582*	(0.321)
Trips 1+ miles = (238,364)	0.730	(0.661)	-0.422	(0.286)
Trips 1+ miles = 365	0.699	(0.687)	- ^b	
Has participated in CBC	1.916***	(0.0706)	0.170	(0.107)
Hunts birds	0.0640	(0.0965)	-0.0767	(0.181)
Gender: Female	-0.169***	(0.0509)	-0.111	(0.107)
Age: 24 years or less	0.539***	(0.0991)	0.994**	(0.424)
Age: 25 to 34 years	0.545***	(0.0871)	0.293	(0.216)
Age: 35 to 44 years	0.360***	(0.0894)	0.325*	(0.192)
Age: 55 to 64 years	-0.207*	(0.110)	-0.117	(0.159)
Age: 65 years and up	-0.298**	(0.134)	0.146	(0.201)
Income: Less than 25K	-0.0590	(0.0853)	-0.0751	(0.254)
Income: 25 K to 50 K	-0.0192	(0.0774)	0.143	(0.150)
Income: 75 K to 100 K	-0.0423	(0.0867)	-0.0150	(0.158)
Income: 100 K or more	-0.0118	(0.0784)	0.143	(0.138)
Region: Northeast	0.164**	(0.0737)	- ^b	
Region: Midwest	-0.0186	(0.0754)	- ^b	
Region: South	0.0552	(0.0660)	- ^b	
Empl. status: Part time	0.0409	(0.0751)	-0.148	(0.188)
Empl. status: Looking for work	-0.173	(0.108)	-0.819	(0.650)
Empl. status: Unemployed	-0.109	(0.0805)	-0.0110	(0.217)
Empl. status: Retired	-0.148	(0.107)	-0.325**	(0.163)
Education: High school	-0.0294	(0.0754)	0.693**	(0.309)
Education: Some college	-0.128*	(0.0671)	0.00246	(0.170)
Education: Masters degree	0.269***	(0.0826)	0.259**	(0.121)
Education: Doctoral degree	0.165	(0.124)	0.00792	(0.165)
cut1	1.279***	(0.113)	-2.651***	(0.288)
cut2	1.895***	(0.116)	-1.309***	(0.279)
cut3	2.258***	(0.119)	-0.363	(0.274)
cut4	2.690***	(0.123)	- ^c	
cut5	3.341***	(0.132)	- ^c	
Observations	4161		572	
Max. log-likelihood	-2390.32		-582.44	

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$ ^aToo few missing. ^bEquals 0 for all. ^cOnly 4 levels.

Female qBus respondents have statistically lower eBird engagement intensities than males, but the same is not true for women in the eBird member survey sample. Individuals who are less than 44 years old have higher propensities to engage with eBird, with the largest effect being for eBird members 24 years of age or younger. Older respondents in the qBus survey have significantly lower eBird engagement propensities.

Income, aggregated into five brackets, does not appear to influence eBird engagement propensity in either sample. However engagement propensities are statistically significantly higher in the Northeast region of the U.S. than elsewhere. In the qBus sample, employment status seems to have no effect on eBird engagement propensities, but in the eBird member survey sample, being retired (as opposed to being employed full time, the omitted category) decreases eBird engagement propensities (where these estimates control for age group and annual frequencies of trips of more than one mile to see birds).

In the qBus sample, compared to individuals with a four-year college degree (the omitted category), those with only some college have lower engagement propensities. For both samples, having a Masters degree increases eBird engagement propensity.²³

4.2.2 Transferring qBus selection model to eBird member survey sample

The main innovation in this paper is the specification of a sample selection model where the selection equation is an ordered-probit model. However, if a conventional selection equation is desired, the six categories in our ordered probit selection model can be aggregated into a simple binary indicator that is 0 for people who are not eBird members (engagement levels 1 and 2) and 1 for eBird members (engagement levels 3, 4, 5 and 6). We can estimate analogous propensity indexes, $Z_i\hat{\gamma}^q$, for either a six-level ordered-probit eBird engagement

²³In our eBird member survey sample, only about 3.5% of respondents have just a high school education or less, so perhaps not much should be read into the statistically significantly positive effect of lower educational attainment on eBird participation propensities in the eBird member survey sample (where respondents were required to be 18 years or older). If school-based eBird projects recruit 18-year-olds still in high school, however, this could account for the greater eBird engagement propensities in this group.

selection model or a binary probit eBird engagement selection model. Online Appendix I digresses to explore a variety of the intermediate components of our models. For example, in terms of in-sample fitted engagement propensities, our ordered-probit selection model tracks the conventional binary-probit selection specification closely when each is applied to the same sample of qBus respondents (although the ordered-probit model predicts somewhat greater propensities at the low end of the range).²⁴

We next use the assumption that for each individual in our eBird member survey sample, we can transfer the relevant set of $\hat{\gamma}^q$ parameters estimated using the qBus data. The qBus selection model to be transferred needs to be estimated using the same set of non-missing regressors, so that we have exactly the necessary information to calculate a predicted propensity index, $Z_j\hat{\gamma}^q$, that exploits as much information as we possess about that individual eBird member’s sociodemographic characteristics. Online Appendix I also includes a comparison of the predicted inverse Mills ratios based on the binary-probit and ordered-probit selection models when the parameters estimated for the qBus sample are transferred to the eBird member survey sample. In this case, the ordered-probit coefficients tend to predict lower IMRs than do the binary-probit coefficients, at least over the upper half of the distribution.²⁵

Figure 1 displays smoothed densities for the marginal distributions across the relevant sample (i.e. the degree of heterogeneity) across respondents in the fitted (or predicted) probabilities of being at each of the four engagement levels (3, 4, 5 and 6), *conditional* on the individual being a member of eBird. Panel A shows the *fitted* individual probabilities of being at each engagement level for the qBus sample. Panel B shows the same for the eBird member survey sample. Panel C shows the *predicted* probabilities of being at each engagement level

²⁴The only adjustment that is necessary for these propensity index measures to be comparable is that the threshold (“cut”) between levels 2 and 3 in the ordered probit model must be normalized to zero (instead of Stata’s default normalization that sets the intercept of the index to zero).

²⁵The selection process for the eBird sample is actually the compound effect of selection into eBird and selection into our sample of survey respondents. To the extent that the sample from our eBird member survey does not represent the population of eBird members, there may be a second layer of selection to consider. We ignore that additional complexity in this paper.

for the eBird member survey sample, calculated by transferring the parameters of the relevant ordered probit model estimated using the qBus sample.

5 Outcome Model: Market Extent, Birding Excursions

5.1 Available variables for outcome model

This section illustrates the use of our predicted, rather than estimated, IMR terms in a model that explains the maximum distance that people state they would typically consider traveling for a one-day birding excursion. This model is estimated using only our eBird member survey sample. This maximum distance reveals the geographical “market extent” for birding excursions, for different types of people. As noted in the introduction, the concept of market extent is related to the topics of distance-decay, spatial preference heterogeneity, and consideration sets for destination choice models. The summary statistics for the eBird-only data available for these models are given in Table 3.

The variables available to use as regressors in our market extent model are different than those used in our binary-probit or ordered-probit models to explain levels of eBird engagement intensity. For our engagement intensity models, we were limited to variables that were available, and could be measured conformably, for both the qBus sample and the eBird member survey sample, because we needed to perform a “model transfer.” We have richer data from the eBird member survey that was not available in the qBus sample. For example, our eBird member survey elicits income in much finer brackets than we could use in the engagement intensity models, so we convert the income bracket data into an approximate continuous income variable.

We also take advantage of our eBird member survey data concerning eBirders’ interests in different species categories. For different categories of bird species, between 6% and 11% of eBirders report that they have no interest in that category. The least popular category in

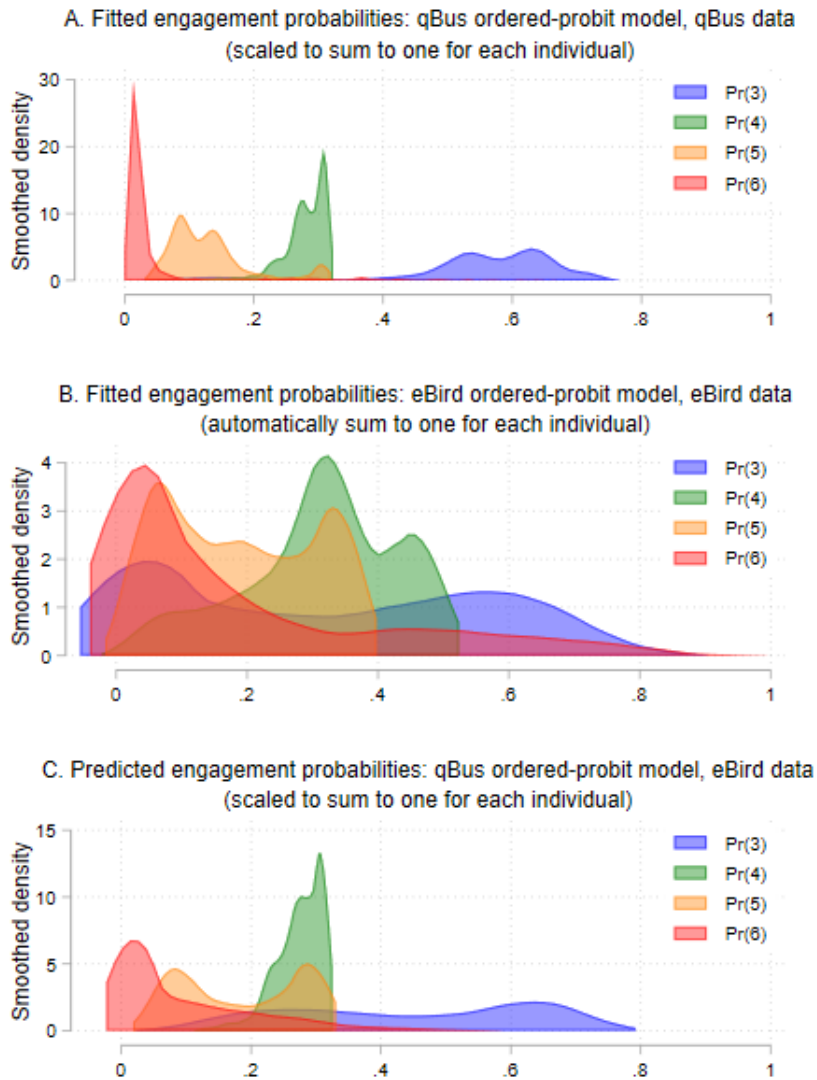


Figure 1: Predicted probabilities for engagement levels 3, 4, 5, and 6. Panel A: fitted engagement level probabilities for qBus sample; Panel B: fitted engagement probabilities for the eBird sample; Panel C: predicted engagement probabilities for the eBird sample, based on an ordered-probit model estimated using the qBus sample.

Table 3: Descriptive statistics: Variables for outcome model, elicited from eBird member survey sample for $n = 1,081$ respondents who answered the question about maximum one-way distance for a birding day-trip

	mean	sd
<i>Dependent variable (market extent, lower bound, chosen interval):</i>		
Self-reported maximum radius of travel in miles	83.283	58.104
<i>Explanatory variables:</i>		
Empl. Status: Employed	0.373	0.484
Income data available	0.804	0.397
Income in 10k, If Reported	7.011	5.891
Gender: Female	0.570	0.495
Age: Less than 45 years	0.171	0.377
Age: More than 64 years	0.367	0.482
Education: Grad school	0.505	0.500
No Interest: Perching birds	0.057	0.233
No Interest: Other game birds	0.111	0.314
<i>Selection-correction options:</i>		
Binary probit IMR	2.035	1.212
Adjusted ordered probit IMR	1.668	0.978
Engagement propensity (demeaned using qBus mean)	0.657	1.261
Observations	1081	

our eBird member sample, for example, is “game birds other than waterfowl” (e.g. pheasants, turkeys, grouse or partridges). This information about the goals of individual birders ties our analysis to the notions explored in Swait et al. (2020), who find that benefit variations associated with distance depend upon people’s goals in their recreational pursuits.

In the specific context of birding, the question of the effective geographical market extent for birders has bearing on the potential “active use” versus “passive use” (option, bequest, or existence) values of environmental projects to protect or enhance local wild bird populations. It is likewise relevant to calculation of the welfare impacts of wholesale shifts in the geographic ranges of different bird species in response to climate change. (Birds are highly mobile and are likely to relocate more quickly than most bird-watchers, especially if climate change accelerates.)

5.2 Estimation results for outcome model

Our dependent variable for these models, the maximum distance considered for a typical one-day birding trip, is elicited in “distance brackets” in our eBird survey. The exact wording of the question is: “If you are NOT making a special trip to try to see a reported rare bird, what is the greatest distance you would consider traveling, one way, for a regular single-day birding trip?” The lowest category is “10 miles or less” so no answers of exactly zero are observed. We thus assume that these distances are strictly positive. Given that the boundaries for these brackets are known, a reasonable estimation method assumes that the latent continuous dependent variable is conditionally lognormally distributed. An interval-data regression model can then be estimated by maximum likelihood methods.²⁶

Model 1 in Table 4 is a naive specification to explain market extent (maximum willingness to travel to see birds) with no corrections. The other columns show several alternative types of corrected models. Model 2 is an otherwise naive specification that employs only our constructed weights, as detailed in Appendix H. Models 3 through 5 continue to employ these weights. Model 3 includes an IMR variable based on a conventional binary-probit selection equation, and Model 4 employs our novel ordered-probit selection equation. Finally, Model 5 shows the results from our ad hoc selection-correction strategy that interacts each main determinant of market extent with a demeaned predicted engagement propensity (based on our adjusted ordered-probit selection specification estimated on the qBus sample and transferred to the eBird member survey sample).²⁷ Ad hoc correction specifications like

²⁶Stata’s `intreg` estimator is available for such models. Were we to resort to FIML estimation of a joint model for the pooled samples, we could possibly entertain an interval regression specification with extra probability at zero. Our survey includes a question that reads: “If you travel more than one or two miles from home to go birding, what is your most frequent mode of travel for these birding trips?” Less than 6% of respondents selected the answer: “I never travel more than one or two miles for birding.” Still, this admits for trips to closer destinations. We could also look for eBird members for whom every birding report is identically geo-located, although we would have to assume that this location was their home, to conclude that their maximum historical travel distance has been zero. Ultimately, the notion of the market extent elicited from our eBird respondents is *prospective*, not revealed from their past behavior, so we do not attempt to implement a zero-inflated interval-regression specification in this study.

²⁷For Models 2 through 5 in Table 4, the weights are designed to correct for differences in observable

Model 5 are potentially helpful in contexts where the error term in the outcome equation does not have an explicit (or at least an underlying) normal distribution—as is the difficulty with most choice models.

In the models reported in Table 4, our explanatory variables include whether the eBird member is currently employed, whether they were willing to report their income in our eBird survey, the level of that income, their gender, their membership in three broad age brackets and two educational attainment categories, as well as whether they specifically express *no* interest in each of two categories of bird species.²⁸

Compared to Model 1, Model 2 employs our calculated sample weights—based on relative fitted engagement-level probabilities in the general population, as opposed to this eBird member survey sample. Recall that women represent about 57% of the eBird sample, but only 51% of the qBus general population sample. The only notable difference in the estimates, with the inclusion of weights, is that the coefficient on the female indicator, which was negative and statistically significant at the 5% level in the unweighted model, becomes statistically insignificant in all other specifications. Given this difference, we retain these weights in subsequent specifications and consider the ways in which the results for Models 3, 4, and 5 are different from those for Models 1 and 2.

determinants of engagement intensities among eBird members, to make this particular sample of eBird members more representative of engagement intensities among eBird members in the general population (i.e. in the qBus sample, in this case).

²⁸Our survey elicited levels of interest in five categories of species, but for only two categories does disinterest have statistically significant effects on market extent. We have also explored other potential explanatory variables, but exclude them because they have persistently statistically insignificant coefficients across a wide variety of specifications.

Table 4: Market extent models without and with engagement-intensity weights and either sample selection corrections or interactions between all regressors and demeaned ordered-probit selection propensity. Dependent variable: logarithm of maximum one-way distance willingly traveled on a typical birdwatching day-trip.

	(1) Naive	(2) Weights only	(3) Probit IMR	(4) Ordered probit IMR	(5) Demeaned propensity ^a
Empl. Status: Employed	-0.0351 (0.0696)	-0.0613 (0.0973)	-0.0872 (0.0943)	-0.0934 (0.0936)	-0.299* (0.154)
Income data available	-0.429*** (0.127)	-0.362** (0.180)	-0.342* (0.176)	-0.354** (0.175)	-0.223 (0.186)
ln(Income in 10K, if reported)	0.218*** (0.0533)	0.171** (0.0730)	0.156** (0.0718)	0.158** (0.0710)	0.0628 (0.0887)
Gender: Female	-0.127** (0.0590)	-0.123 (0.0796)	-0.0374 (0.0787)	-0.0410 (0.0783)	0.000944 (0.106)
Age: Less than 45 years	0.185** (0.0835)	0.225** (0.112)	0.167 (0.106)	0.137 (0.108)	-0.317 (0.197)
Age: More than 64 years	-0.0489 (0.0713)	-0.114 (0.0982)	-0.0287 (0.100)	-0.103 (0.0961)	-0.0110 (0.115)
Education: Grad school	0.113* (0.0598)	0.0132 (0.0751)	-0.0649 (0.0741)	-0.0642 (0.0748)	-0.259*** (0.0958)
No Interest: Perching birds	-0.811*** (0.148)	-0.862*** (0.198)	-0.847*** (0.205)	-0.829*** (0.202)	-0.749*** (0.190)
No Interest: Other game birds	-0.634*** (0.107)	-0.660*** (0.130)	-0.577*** (0.131)	-0.578*** (0.130)	-0.549*** (0.127)
Binary probit IMR			-0.169*** (0.0305)		

Continued on next page

Ordered probit IMR					-0.386*** (0.0689)
Empl. Status: Employed × Eng. prop (demeaned)					0.185 (0.158)
Income data avail. × Eng. prop (demeaned)					-0.120 (0.0756)
ln(Income in 10K, if reported) × Eng. prop (demeaned)					0.134* (0.0692)
Gender: Female × Eng. prop (demeaned)					0.224* (0.117)
Age: Less than 45 years × Eng. prop (demeaned)					-0.00451 (0.0733)
Age: More than 64 years × Eng. prop (demeaned)					-0.0223 (0.0607)
Education: Grad school × Eng. prop (demeaned)					0.0176 (0.0551)
No Int.: Perching birds × Eng. prop (demeaned)					-0.231 (0.175)
No Int.: Other game birds × Eng. prop (demeaned)					0.160 (0.107)
Engagement propensity (demeaned using qBus mean)					0.282*** (0.0813)
Constant	4.066*** (0.0972)	4.170*** (0.127)	4.494*** (0.135)	4.403*** (0.131)	4.102*** (0.140)
Insigma Constant	-0.0803*** (0.0237)	-0.0583* (0.0306)	-0.0788** (0.0313)	-0.0808*** (0.0310)	-0.105*** (0.0310)
Observations	1081	1081	1081	1081	1081

Continued on next page

Log Likelihood	-2411.41	-2429.96	-2409.82	-2408.03	-2382.37
AIC	4844.83	4881.92	4843.64	4840.05	4806.74
BIC	4899.67	4936.77	4903.47	4899.88	4911.44
Weighted?	No	Yes	Yes	Yes	Yes

Note: Standard errors in parentheses. * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

^a Not shown for Model (5): the rest of the full set of interactions with demeaned predicted engagement propensity. None of these other interactions bear coefficients that are statistically significantly different from zero.

IMR coefficients. Models 3 and 4 in Table 4 are the two IMR-based selection-corrected models that rely on the strong assumption of bivariate normal errors for the latent engagement intensity variable and the interval-censored outcome variable. The coefficient of interest is that on the relevant fitted inverse Mills ratio. In two-stage methods, this coefficient is the estimate of $\rho\sigma_\epsilon = \beta_\lambda$, as in equation (3). Given that the error standard deviation, σ_ϵ , must be positive, the sign of this compound parameter implies the sign of ρ , the correlation between the errors in the selection and outcome equations.

Our negative IMR coefficients in Models 3 and 4 imply that unobserved factors that make a respondent *more* likely to be intensely engaged with eBird also make them willing to travel *less* far on a typical one-day birding trip. Models 3 and 4 do, however, treat these second-step fitted IMR variables as non-stochastic (thereby understating the amount of noise in the model). Nevertheless, these negative IMR coefficients are strongly statistically significantly different from zero.²⁹

A priori, we expected (if anything) that the propensity to participate in eBird would be positively associated with the outcome variable that we consider in this analysis, since latent birding avidity could be a potentially important omitted variable. It is thus somewhat counter-intuitive to find negative coefficients on our sample-selection correction terms. Instead of birding avidity, the relevant unobserved heterogeneity might include the opportunity cost of time (or perhaps unobserved age-related technical sophistication in using the online eBird app, or online surveys in general).

Employment status. None of Models 1 through 4 in Table 4 suggest that employment status has a statistically significant effect on the market extent for birders. However, Model 5, using our ad hoc correction of interacting each of the regressors with the demeaned engagement propensity variable, suggests that for the general population, market extent is

²⁹FIML estimation of the joint model for engagement propensity and market extent could remedy this problem and should be pursued in future applications where hypothesis testing is particularly important for policy.

smaller by about 30% if the respondent is currently employed. This is not surprising. Employed individuals are likely to have less free time for all leisure activities, including birding day-trips.

Income availability indicator and level of income, if known. For all but Model 5, compared to respondents who decline to provide such data in the eBird member survey, those who do provide income data report a market extent that is smaller by about 34% to 43%. However, this negative effect in these specifications is offset by the positive effect of income (when reported) on market extent—a 1% higher income corresponds to an market extent that is larger by about 0.15% to 0.22%. This may seem plausible because higher-income respondents likely have less-binding budget constraints for travel expenses.³⁰ However, Model 5 suggests that in the general population, income has no statistically discernible effect on the market extent for birding trips.

Gender. The point estimate for the effect of being female on market extent is estimated to be negative in Models 1 through 4 (although the estimate is statistically significantly negative in Model 1). The estimated effect of gender changes sign in Model 5, but remains insignificant, suggesting that gender has no effect on market extent in the general population.

Age. Models 1 and 2, which do not correct for systematic selection, suggest that being less than 45 years old (compared to the omitted category of 45 to 64 years old) is associated with a market extent that is larger by about 18% to 23%, but this effect disappears in Models 3 through 5 that explore alternative remedies for systematic selection.

Education. Relative to the omitted category of eBird members with college degrees or less, Model 1 implies that having attended at least some graduate school increases expected market extent by 11%, significant at the 10% level. Models 2 through 4 suggest that graduate

³⁰Compared to respondents who withhold their income data, the positive effect of greater income overcomes the negative effect associated with the provision of any income data when income reaches roughly \$21,400 to \$26,200. Mean reported household income in the sample is about \$87,200, and the minimum reported income is \$18,000, so the effect of additional income on maximum travel distance is positive for most of the sample.

school has no statistically significant effect on market extent, but Model 5 implies that in the general population, graduate school is actually associated with a strongly statistically significant 26% *smaller* market extent.

Disinterest in particular categories of species. Across all five specifications, respondents to our eBird member survey who reveal that they are *not* interested in perching birds or not interested in “other game birds” (i.e. game birds other than waterfowl), have statistically significantly smaller market extents. The magnitudes of these effect are also similar across all specifications. Reporting a lack of interest in either of these categories of birds shrinks expected market extent substantially, by 58% to 86%.

Model 5’s interaction terms. Among the selection-correction models, Models 3 and 4 rely upon a strong assumption of bivariate normal errors and slope coefficient that are identical in the eBird sample and the general population. Under these specific conditions, adding to the model a single (appropriate) IMR term, with an unrestricted coefficient, would yield slope coefficients for the other explanatory variables that are uncontaminated by sample selection. The inverse Mills ratio strategy can be described as a structural approach to sample selection correction.

In contrast, Model 5 is ad hoc, unstructured and highly flexible. This approach makes a different, but perhaps equally strong assumption—that each of the parameters of the outcome model varies linearly with the respondent’s predicted propensity to engage with eBird, the latent continuous variable that drives both the binary-probit model for eBird membership, and the richer ordered-probit model that we employ to explain differences in people’s intensive margin of participation in eBird (at various engagement levels). The linear relationship between each estimated coefficient and the predicted engagement propensity may be positive or negative or statistically zero. The counterfactual we wish to simulate is the set of outcome-model parameters that would obtain if everyone in the estimating sample shared the mean engagement propensity in the general population.

Prior to estimation, we have transformed each respondent’s predicted engagement propensity (the $Z_j\hat{\gamma}^q$ “index”) by taking its deviation from the population mean (i.e. from its mean in the qBus sample, the average value of $Z_i\hat{\gamma}^q$). In the population, the demeaned engagement propensity variable would be zero, but our estimating sample is not representative of that population. In Table 3, note that the average demeaned engagement propensity in the estimating sample is positive, at about 0.657. The people who appear in our estimating sample from our eBird member survey understandably have a higher-than-average propensity to engage with eBird.

When we have included in Model 5 the interaction terms between each basic regressor and our demeaned engagement propensity variable, the coefficients on the non-interacted basic regressors in the outcome model can be interpreted as the simulated values of those coefficients *at the mean engagement propensity in the population*. In the bottom half of Table 4, for Model 5, we show the estimated coefficients on the interaction terms, which reveal how the effects of each basic regressor vary systematically with the individual’s predicted engagement propensity, where that predicted engagement propensity is based on our adjusted ordered-probit engagement intensity model.

The interaction terms in Model 5 suggests that while income has no statistically discernible effect on market extent at the mean engagement propensity in the general population, the effect of income on market extent increases systematically with the respondent’s predicted engagement propensity. There is a similar effect for being female. The most statistically significant interaction term in Model 5, however, is the (implicit) interaction between the demeaned engagement propensity variable and the intercept term in the basic specification. This interaction is just the demeaned engagement propensity variable itself. The strongly statistically significant positive coefficient on this term implies that expected market extent is larger as the demeaned engagement intensity increases. Given that demeaned engagement intensity in the estimating sample has an average value that is positive, the

eBird member survey sample, without correction, overstates the market extent for birding in the general population.

One important observation about the demeaned engagement propensity variable in Model 5 is that the ordered-probit inverse Mills ratio is very close to being a linear transformation of this variable over the relevant range in our data. The correlation between the two variables is -0.9955. For corrected predictions about market extent in Model 4, we eliminate the IMR term by setting its *coefficient* to zero (i.e. by assuming that ρ is zero, so that $\rho\sigma_\epsilon = 0$). In Model 5, if we were to include just the demeaned engagement propensity variable without its interactions with the basic regressors, we would zero out the demeaned propensity variable itself to produce corrected predictions about market extents. Given the degree of correlation between the two variables, either type of correction would be expected to have about the same effect on the vector of coefficients on the basic variables. Thus we can view Model 5 as being, in effect, a generalization of Model 4, with additional flexibility to permit not only the intercept to differ (with either the inverse Mills ratio or the demeaned engagement intensity), but all the slopes as well.

5.3 Predicted values for the outcome variable, with and without corrections

The point of correcting for systematic sample selection is to adjust the statistical relationships observed in the selected sample to better reflect the general population. In this section, we compare the predicted market extents for selected specifications.³¹ The top graph in Figure 2 shows the predicted market extent from Model 4 in Table 4 plotted against the predicted market extent for the same observations under the naive Model 1 with no weighting or

³¹Recall that the dependent variable in the specifications in Table 4 is in log form. Exponentiation of a fitted log value yields the median of the fitted level. One must multiply by the fitted value of $(\sigma^2/2)$ to recover the mean of the fitted conditional distribution, due to the skewness of the implied log-normal distribution.

any correction for sample selectivity in the eBird citizen science sample. Model 4, with its ordered-probit inverse Mills ratio term, predicts market extents that are uniformly larger than those predicted by Model 1. This difference arises because of the negative error correlation between the selection equation and the outcome equation, as implied by the negative coefficient on the inverse Mills ratio term. An individual who is more likely to show up in the eBird sample than their observed characteristics would predict also tends to have a smaller market extent than their characteristics would predict.

However, the effects of systematic selection on predicted market extents implied by Model 4 are notably opposite from the effects implied by the results shown in the bottom graph in Figure 2. This second graph features the market extents predicted by Model 5 in Table 4, where each explanatory variable is also interacted with the demeaned engagement propensity variable. This demeaned propensity is then set to zero to simulate the expected market extent if everyone in the sample had a fitted engagement intensity equal to the average in the qBus sample. These fitted values, likewise plotted against those for the naive Model 1, show that the market extents in the general population are smaller than they are in the selected sample of birding enthusiasts in the eBird sample. The pattern of clustering in these predicted values stems from the fact that the demeaned engagement propensity is a function mostly of indicator variables, and the interaction terms in the model for market extents are likewise mostly indicator variables. Clearly, effect of the negative error correlation between the selection and outcome equations is more than offset by the heterogeneity in the slope coefficients that is a function of predicted engagement propensities.

Figure 3 compares the two marginal distributions of predicted market extents for birding trips, with and without selection corrections. It is unsurprising that basing estimates of market extents for one-day birding excursions on a sample of eBirders would likely overpredict market extents for such trips in a general population sample with the same characteristics. However, the absence of a spike at zero in Figure 3 is notable, given that roughly 12% of

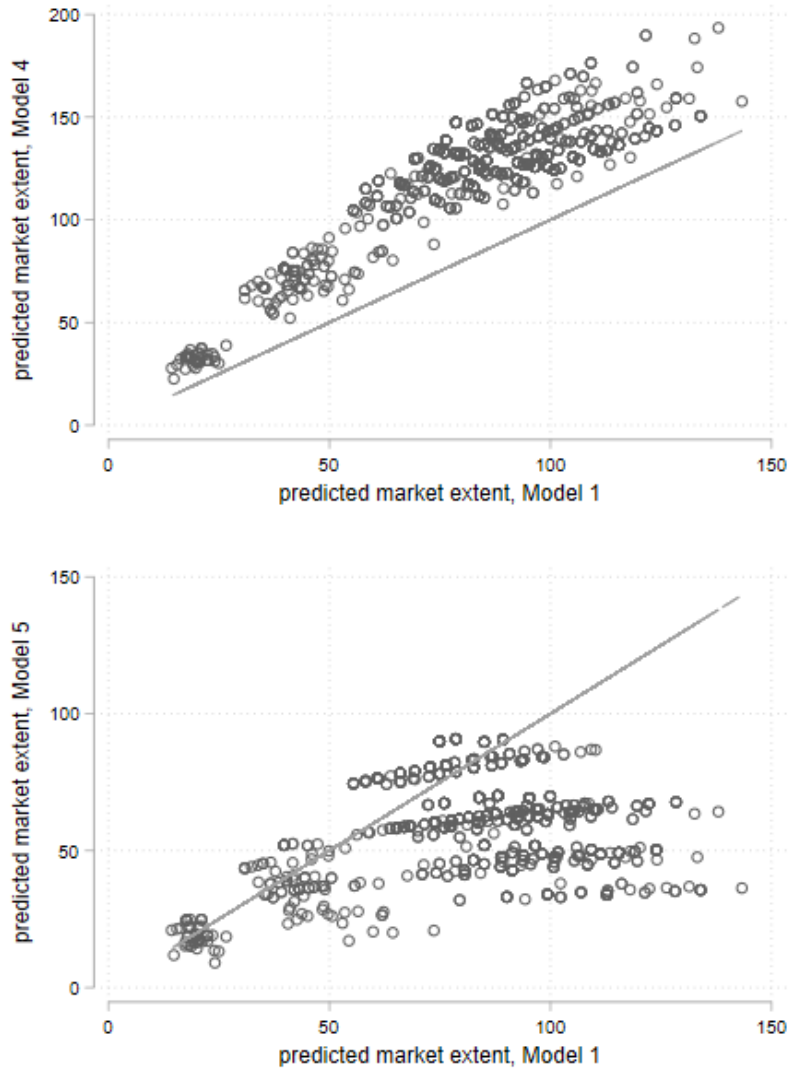


Figure 2: Predicted market extent for 1,081 observations in the eBird sample based on Model 4 versus Model 5 in Table 4 plotted against the predicted market extent from the naive Model 1 (45-degree lines added).

the general population that does not report even incidental attention to wild birds over the past year. The absence of a point mass at zero for our eBird data on subjective market extents probably means that our corrected estimates cannot be scaled to 100% of the overall population. These market extents will likely be relevant for a subset of the population.³²

Which subset? In our qBus sample, we find that about 67% of respondents report having traveled more than one mile to see birds on at least one day during the last year, so perhaps that share of the general population is relevant for scaling our corrected distributions. However, we also note that the 2016 Survey of Fishing, Hunting and Wildlife-Associated Recreation, with the stratified sampling in its screener survey, finds that only about 18% of that sample reports traveling more than one mile from home to observe wildlife, so it may be important to investigate further the degree of sample selection bias that may be present in FHWAR samples. Either way, the fact that less than 12% of our general-population qBus respondents report being either an active or an inactive member of the eBird CS project, it is clear that the possibility of systematic selection bias in CS data should always be explored.

6 Conclusions and Recommendations

We intersect the sample selection literature and the literatures on market extents, distance-decay, spatial preference heterogeneity and consideration sets. Our goal is to augment the research tool-kit for using citizen science data—with improved confidence that any insights to be derived are more suitable for scaling to the general population or for use in benefits transfer exercises. The two main tasks in the paper are to (1) illustrate some new sample selection correction techniques we have developed to allow for the use of data from auxiliary

³²Nevertheless, we note that even market extents of zero, for actual travel away from home to enjoy “active use” of wild birds, do not preclude the possibility of “passive use” values (option, bequest, or existence values) for wild birds in the region. Birds are also mobile, not just people. The presence of wild birds within any given market extent will also affect the probability that these birds may be viewed in one’s backyard, without the necessity of travel.



Figure 3: For 1,081 eBird member survey observations: Marginal distribution of predicted market extents according to our naive Model 1 overlaid by selection-corrected predictions of market extents for (birders in) the general population based on Model 5.

general-population surveys to correct for sample selection present in citizen science data, and (2) model the market extent of regular bird-watching day-trips in Oregon and Washington states, as an illustration. Our contrasting results for the market-extent model demonstrate that corrections for sample selection (and weighting for engagement intensity) may be very important for scaling to the general population, or transferring to other contexts, any results derived from citizen science data.

The key takeaway from our illustrative market-extent “outcome” model is the potential importance of non-random selection into citizen science projects. Preferences in the general population are important if government agencies, for example, are to make good decisions about the efficient allocation of resources to protect wild birds, a public good. How to provide the appropriate amount of wild bird habitat is an increasingly relevant policy question because land-cover change and climate change present significant threats to wild bird populations. Changes in bird populations will affect birdwatcher welfare (see Kolstoe et al. (2018)

for an illustrative example). To limit the loss of bird populations and bird biodiversity, multiple agencies at all levels of government will likely need to work together.

It is important to recognize—especially in the case of migratory species such as birds—that actions in one location have the potential to affect outcomes at other locations. Existing programs, such as the National Wildlife Refuge System and the Urban Bird Treaty Program, make a good start but appear not to have been sufficient, given that avian biodiversity remains a concern (in light of changes in land cover and the climate). Conservation solutions must account for the fact that political jurisdictions may not align with the spatial “market extent” for non-market demands for conservation (a concern also explored by Bakhtiari et al. (2018) and Vogdrup-Schmidt et al. (2019)).

The need for a qBus-type sample to permit sample selection corrections in this instance highlights the potential value of broad-based surveys of bird-watching trip behavior and citizen-science engagement. Information about trip-taking behavior has long been gathered by the U.S. Fish and Wildlife Service through their quinquennial general-population survey on Fishing, Hunting and Wildlife Watching. However, as of 2016, the information began to be reported only at the census division level, rather than the state level, as had been the case for prior waves of the survey. The loss of geographic resolution due to this decision limits the usefulness of FHWAR information for city-, county- and state-level government agencies.

The FHWAR survey is perhaps the most appropriate existing survey to which a detailed question could be added about participation in outdoor-based CS projects (assuming U.S. Fishing, Hunting & Wildlife Watching Survey continues in the future). Also, given that the federal registry now documents more than 400 CS projects (see www.citizenscience.gov), general-population information on CS participation would benefit other agencies, such as the National Oceanic Atmospheric Administration (NOAA) or US Geological Survey (USGS), which could also exploit data from CS projects on recreational behavior. Such CS projects

include Watch for Whales (NOAA), Geocache for a Good Cause (NOAA), and Nature's Notebook (USGS), for example.

To be most useful, existing general-population surveys could (and should) include questions about citizen science engagement in projects related to ecosystems services that are valued for active recreational activities. This general-population engagement information would be a vital complement to any special-purpose surveys fielded to members of CS projects to help researchers understand both active and passive use values for a wide range of environmental public goods. Without general-population information, it will continue to be very difficult to scale to the general population any empirical findings based solely on surveys fielded to “convenience samples” of CS participants.

References

- Badura, T., S. Ferrini, M. Burton, A. Binner, and I. J. Bateman (2020). Using individualised choice maps to capture the spatial dimensions of value within choice experiments. *Environmental Resource Economics* 75(2), 297–322.
- Bakhtiari, F., J. B. Jacobsen, B. J. Thorsen, T. H. Lundhede, N. Strange, and M. Boman (2018). Disentangling distance and country effects on the value of conservation across national borders. *Ecological Economics* 147, 11–20.
- Bateman, I. J., B. H. Day, S. Georgiou, and I. Lake (2006). The aggregation of environmental benefit values: Welfare measures, distance decay and total wtp. *Ecological Economics* 60(2), 450–460.
- Cameron, T. A. and J. DeShazo (2013). Demand for health risk reductions. *Journal of Environmental Economics and Management* 65(1), 87–109.
- Cameron, T. A. and J. Englin (1997). Respondent experience and contingent valuation of environmental goods. *Journal of Environmental Economics and Management* 33(3), 296–313.
- De Valck, J. and J. Rolfe (2017). Spatial heterogeneity in stated preference valuation: Status, challenges and road ahead. *International Review of Environmental and Resource Economics* 11(4), 355–422.
- Dundas, S. J. and R. H. von Haefen (2020). The effects of weather on recreational fishing demand and adaptation: Implications for a changing climate. *Journal of the Association of Environmental and Resource Economists* 7(2), 209–242.
- Greene, W. H. (2012). *Econometric Analysis (7 th)*. Upper Saddle River, NJ: Prentice Hall.
- Heckman, J. J. (1979). Sample selection bias as a specification error. *Econometrica: Journal of the econometric society*, 153–161.
- Holland, B. M. and R. J. Johnston (2017). Optimized quantity-within-distance models of spatial welfare heterogeneity. *Journal of Environmental Economics and Management* 85, 110–129.
- Jank, W. and P. K. Kannan (2005). Understanding geographical markets of online firms using spatial models of customer choice. *Marketing Science* 24(4), 623–634.
- Johnston, R. J. and A. S. Abdulrahman (2017). Systematic non-response in discrete choice experiments: implications for the valuation of climate risk reductions. *Journal of Environmental Economics and Policy* 6(3), 246–267.
- Johnston, R. J., E. Y. Besedin, and B. M. Holland (2019). Modeling distance decay within valuation meta-analysis. *Environmental Resource Economics* 72(3), 657–690.

- Keeler, B. L., S. A. Wood, S. Polasky, C. Kling, C. T. Filstrup, and J. A. Downing (2015). Recreational demand for clean water: evidence from geotagged photographs by visitors to lakes. *Frontiers in Ecology and the Environment* 13(2), 76–81.
- Kolstoe, S. and T. A. Cameron (2017). The Non-market Value of Birding Sites and the Marginal Value of Additional Species: Biodiversity in a Random Utility Model of Site Choice by eBird Members. *Ecological Economics* 137, 1–12.
- Kolstoe, S., T. A. Cameron, and C. Wilsey (2018). Climate, land cover, and bird populations: Differential impacts on the future welfare of birders across the pacific northwest. *Agricultural and Resource Economics Review* 47(2), 272–310.
- Logar, I. and R. Brouwer (2018). Substitution effects and spatial preference heterogeneity in single- and multiple-site choice experiments. *Land Economics* 94(2), 302–322.
- Loomis, J. B. (1996). How large is the extent of the market for public goods: evidence from a nationwide contingent valuation survey. *Applied economics* 28(7), 779–782.
- Newbold, S., R. D. Simpson, D. M. Massey, M. T. Heberling, W. Wheeler, J. Corona, and J. Hewitt (2018). Benefit transfer challenges: Perspectives from us practitioners. *Environmental Resource Economics* 69(3), 467–481.
- Olsen, R. J. (1980). A least-squares correction for selectivity bias. *Econometrica* 48(7), 1815–1820.
- Roberts, A. J., P. K. Devers, S. Knoche, P. I. Padding, and R. Raftovich (2017). Site preferences and participation of waterbird recreationists: Using choice modelling to inform habitat management. *Journal of Outdoor Recreation and Tourism-Research Planning and Management* 20, 52–59.
- Rodrigue, J.-P., C. Comtois, and B. Slack (2016). *The geography of transport systems*. Routledge.
- Rosenberg, K. V., A. M. Dokter, P. J. Blancher, J. R. Sauer, A. C. Smith, P. A. Smith, J. C. Stanton, A. Panjabi, L. Helft, M. Parr, and P. P. Marra (2019). Decline of the north american avifauna. *Science*.
- Sessions, C., S. A. Wood, S. Rabotyagov, and D. M. Fisher (2016). Measuring recreational visitation at us national parks with crowd sourced photographs. *Journal of Environmental Management* 183, 703–711.
- Smith, V. K. (1993). Nonmarket valuation of environmental resources: An interpretive appraisal. *Land Economics* 69(1), 1–26.
- Sonter, L. J., K. B. Watson, S. A. Wood, and T. H. Ricketts (2016). Spatial and temporal dynamics and value of nature-based recreation, estimated via social media. *PLoS one* 11(9), e0162372.

- Swait, J., C. Franceschinis, and M. Thiene (2020). Antecedent volition and spatial effects: Can multiple goal pursuit mitigate distance decay? *Environmental Resource Economics* 75(2), 243–270.
- Terza, J. V. (1998). Estimating count data models with endogenous switching: Sample selection and endogenous treatment effects. *Journal of Econometrics* 84(1), 129–154.
- Terza, J. V. (2009). Parametric nonlinear regression with endogenous switching. *Econometric Reviews* 28(6), 555–580.
- Vella, F. (1998). Estimating models with sample selection bias: a survey. *Journal of Human Resources*, 127–169.
- Vogdrup-Schmidt, M., A. L. Abatayo, J. F. Shogren, N. Strange, and B. J. Thorsen (2019). Factors affecting support for transnational conservation targeting migratory species. *Ecological Economics* 157, 156–164.
- von Haefen, R. H. (2008). Latent consideration sets and continuous demand systems. *Environmental Resource Economics* 41(3), 363–379.
- Walsh, P. J., J. W. Milon, and D. O. Scrogin (2011). The spatial extent of water quality benefits in urban housing markets. *Land Economics* 87(4), 628–644.
- Wood, S. A., A. D. Guerry, J. M. Silver, and M. Lacayo (2013). Using social media to quantify nature-based tourism and recreation. *Scientific reports* 3, srep02976.
- Wooldridge, J. M. (2002). *Econometric Analysis of Cross Section and Panel Data*. MIT Press.-2002.
- Yuan, Y., K. J. Boyle, and W. You (2015). Sample selection, individual heterogeneity, and regional heterogeneity in valuing farmland conservation easements. *Land Economics* 91(4), 627–649.

Complete Table of Contents for paper, plus Online Appendices to accompany:

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for Sample-Selection Correction in Models Based on
Crowd-sourced Volunteered Geographic Information**

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Appendices

(Online supplementary material)

A Birding activity variables for qBus and engagement intensity options for both qBus and eBird samples

Table A1: Share of 1050 qBus respondents reporting at least one day over the last year of engagement with the following wild-bird-related activities (response format: slider with labels at 0, 61, 122, 183, 243, 304 and 365 days); mean days per year and lower and upper quartiles of days. We find these counts to be rather high. This may be an artifact of using the Qualtrics' sliders to elicit numbers of days.

Description	N	At least 1 day	Mean days/ year	Lower quartile (days)	upper quartile (days)
<i>Positive non-consumptive engagement with wild birds:</i>					
Pause what you are doing to observe wild birds	999	0.881	92.8	10	161
Put out food for wild birds	960	0.783	98.4	3	181
Seek opportunities to learn more about wild birds	940	0.728	69.7	0	112
Photograph wild birds	945	0.747	68.5	0	107
Visit public parks/areas less than one mile from home to see, photograph or feed wild birds	926	0.703	67.2	0	109
Travel more than one mile from home to see, photograph or feed wild birds	914	0.667	62.4	0	90
— Any days, any of the above?	1050	0.878	-	-	-
<i>Other interactions with wild birds:</i>					
Employ measures to keep wild birds from harming your garden or property	910	0.624	60.3	0	92
Hunt wild birds for sport or for food	895	0.517	49.7	0	48

Table A2: Definitions and values of two eBird engagement variables for our two samples. CS is the dependent variable for the binary probit selection model; $CS6$ is the dependent variable for the six-level ordered-probit selection model (where $CS6$ degenerates to a four-level model for the eBird sample used alone).

eBird engagement bins	CS values	$CS6$ values	Observed for qBus general population sample?	Observed for eBird citizen science sample?
Does not know eBird	0	1	Y	N
Knows eBird, not a member	0	2	Y	N
Member, reports rarely	1	3	Y	Y
Member, reports < half	1	4	Y	Y
Member, reports > half	1	5	Y	Y
Member, reports almost all	1	6	Y	Y

B Review of the usual context for Heckman's two-stage binary selection correction

For the qBus general population panel, consider a binary indicator for eBird participation CS_i and a set of available regressors Z_i , for a representative sample. If we also had data, for these eBird participants, on an outcome variable of interest, y_i , and a set of regressors, X_i for a subset of this same sample, we would proceed as follows. Suppose the latent propensity to participate in eBird in this qBus sample is a linear-in-parameters function of the Z_i variables, $CS_i^* = Z_i\hat{\gamma} + \eta_i$, then the standard Heckman two-step sample-selection correction procedure involves two terms constructed from $Z_i\hat{\gamma}$.³³ Define:

$$\begin{aligned}\lambda(\alpha_{CS_i}) &= \lambda(-Z_i\hat{\gamma}) = \frac{\phi(-Z_i\hat{\gamma})}{1 - \Phi(-Z_i\hat{\gamma})} = \frac{\phi(Z_i\hat{\gamma})}{\Phi(Z_i\hat{\gamma})} \\ \delta(\alpha_{CS_i}) &= \delta(-Z_i\hat{\gamma}) = \lambda(-Z_i\hat{\gamma}) [\lambda(-Z_i\hat{\gamma}) - (-Z_i\hat{\gamma})]\end{aligned}\tag{4}$$

With sample selection, the conditional expected value and the error variance of the outcome variable y_i are no longer given simply by $E[y_i] = X_i\beta$ and $Var[y_i] = \sigma_y^2$. Instead, we need the expected value and variance of the *marginal* distribution of y_i *conditional* on y_i being observed (i.e. when $CS_i = 1$). If we can assume that the latent propensity variable CS_i^* is distributed bivariate normal with the outcome variable y_i , but the joint distribution is truncated below at $-Z_i\hat{\gamma}$ in the CS_i^* dimension, the formulas for the expected value and variance of the relevant marginal distribution of y_i for this singly truncated bivariate normal distribution are as follows, as in Greene (2012, p. 836):

$$\begin{aligned}E[y_i|y_i \text{ observed}] &= E[y_i|CS_i^* > -Z_i\hat{\gamma}] = X_i\beta + \rho\sigma_\epsilon\lambda(-Z_i\hat{\gamma}) = X_i\beta + \beta_\lambda\lambda(-Z_i\hat{\gamma}) \\ Var[y_i|y_i \text{ observed}] &= Var[y_i|CS_i^* > -Z_i\hat{\gamma}] = \sigma_y^2 [(1 - \rho^2)\delta(-Z_i\hat{\gamma})]\end{aligned}\tag{5}$$

These formulas provide the rationale for the Heckman two-step approach and why, once this augmented second-stage model has been estimated, we would have unbiased estimates of the expected value of y_i when y_i is observed under the counterfactual conditions where the correlation between the errors in these two equations is zero. For *uncorrelated* bivariate normal variables, the conditional distributions are everywhere equal to the marginal distribution, so we want to *simulate* the absence of any such error correlation. Based on the augmented regression model, therefore, we can set $\rho = 0$ to get:

$$\begin{aligned}E[y_i|y_i \text{ observed}] &= X_i\beta + (0\sigma_\epsilon)\lambda(-Z_i\hat{\gamma}) = X_i\beta \\ Var[y_i|y_i \text{ observed}] &= \sigma_y^2 [(1 - (0)^2)\delta(-Z_i\hat{\gamma})] = \sigma_y^2\end{aligned}\tag{6}$$

³³Typically, however, attention is focused primarily on the λ term.

C Legitimate use of simple Inverse Mills Ratios to correct for sample selection in two-step methods

Over the last several decades, empirical researchers have become accustomed to the idea that estimating a sample-selection model via maximum likelihood methods, calculating the IMR, and including that estimated IMF into the desired “outcome” equation of interest will (somehow) purge the parameters of that outcome equation of any bias due to sample selection. However, it is crucial to remember that the IMR offers an appropriate correction for sample-selection bias only under some very specific conditions. Confidence that “including an IMR term” will “fix” selection bias hinges on the assumption that the selection equation and the outcome equation have error terms that are jointly normally distributed.

The joint normality assumption is critical because the IMR correction derives entirely from the formula for the expected value of a singly truncated bivariate normal distribution. If the conditional distribution latent variable in the selection equation is not normal or the conditional distribution of the dependent variable in the outcome equation is not normal (either observed or censored in some way, perhaps after some transformation), then the needed expected value of the singly truncated joint distribution of the errors in the selection equation and the outcome equation cannot automatically be assumed to be given by the usual IMR formulas.

Ideally, selection and outcome equations should be estimated jointly, in which case a wide variety of joint distributions for the two error terms can be assumed/employed, provided that the joint density can be derived and written down. In some cases, it is convenient to write the conditional joint distributions of the selection propensity and the outcome variable as the product of a conditional distribution and a marginal distribution.³⁴

This insight is especially relevant for researchers who wish to estimate conditional logit “outcome” models based on people’s choices across alternatives with different attributes. Nothing stops the analyst from estimating a binary probit sample selection model and calculating the usual IMR term from the fitted parameters. However, there is no rigorous statistical rationale for including this fitted IMR term like other respondent characteristics as a variable that might shift one or more slope characteristics or the coefficient on the status quo indicator variable, as is done in Yuan et al. (2015). Some types of joint models where IMR correction terms can make sense, statistically, include the following:

- The usual OLS outcome regression with a continuous dependent variable that is con-

³⁴Stata now includes the “heckpoisson” estimator, following Terza (1998). Appropriately, this estimator is available only as a FIML estimator, not as a two-step estimator that relies on an IMR term. Jointly distributed variables that are not both normal have also been used in a FIML model that combines a participation/experience variable (that is distributed either Poisson or zero-inflated-Poisson) with a censored-normal outcome variable is estimated jointly in Cameron and Englin (1997).

ditionally normal, perhaps after some transformation

- A Tobit outcome model (censored anywhere—at the bottom, the top, or both) which involves a partially censored normal propensity variable
- An interval-data outcome variable censored between known thresholds (used in the present paper)
- An ordered-probit outcome model with a normally distributed latent propensity variable
- A censored normal outcome model with different censored points across observations

Simply appending an estimated IMR variable to a second-step outcome equation of interest cannot be assumed to be correct in any of the following cases:

- Count data models: Poisson, negative binomial
- Conditional logit models: fixed or random parameters
- Any other statistical model for the “outcome” equation, where the (perhaps latent) dependent is not conditionally normally distributed (even after transformation)

We note, however, the insights provided in Terza (2009), who describes a general approach to endogenous switching models, endogenous treatment models, and sample selection models. These techniques are extended versions of an approach proposed in Olsen (1980), suitable for within-sample corrections, but they seem not yet to have been widely employed in the empirical literature, especially in environmental economics. Should they become available as pre-coded general commands in commonly used software, these methods would likely be popular. However, they would need to be tailored specially for selection-model transfer exercises such as the two-step illustration in this paper.

D Complementary method: Weights based on predicted engagement intensities

In this section, we focus on the actual eBird members in the qBus sample, comparing their different participation levels to those in the entire eBird sample. With our eBird member survey data, there is the added concern that the *intensity* with which these survey respondents engage with the eBird citizen science project may not be representative of the distribution of eBird engagement propensities in the general population of the U.S. To address this issue, we consider how to develop weights for each of the four levels of participation intensity among these eBird members. We base our weights on the *fitted probabilities* of a respondent being each of the four engagement intensity bins in each sample.

For the qBus sample, we estimate an ordered probit model for all six possible bins and calculate a set of fitted probabilities for each bin for each person, conditional on the Z_i vector for that person. Call these probabilities \hat{p}_{ki} for engagement levels $k = 1, \dots, 6$.

We then make two calculations for each respondent in the eBird member survey sample. In the first calculation, we use the six-level engagement-intensity model estimated using the qBus data to predict (for the eBird member survey sample) the individual-specific set of six probabilities associated with each of the six engagement-intensity bins (even though nobody in the eBird sample is in non-participation bins 1 or 2). Call these fitted probabilities \hat{p}_{kj}^* for engagement levels $k = 1, \dots, 6$,

In the second calculation, we use the eBird sample independently, with its four possible participation-intensity bins. We estimate a four-level ordered-probit model using just the eBird member survey sample and calculate four fitted probabilities, which we will call \hat{q}_{kj} , for engagement levels $k = 3, \dots, 6$ represented in that sample.

The next step is to assign weights to each respondent in the eBird dataset. These weights serve to scale the fitted probability of an individual being in their observed engagement-intensity bin to match the fitted probability in the population (i.e. the qBus sample). First, consider a hypothetical case where everyone in the qBus and eBird samples has been drawn from the same general population and people in both samples thus shared the same mixes of characteristics (i.e. had identical joint distributions for their Z variables). Then we would expect, across the two samples, to have roughly the same proportions of people in each engagement-intensity bin. However, since nobody in the eBird sample is observed in bins 1 or 2, we must focus on the portion of the engagement-intensity distribution corresponding to eBird membership. For the qBus sample, we should consider the probabilities of being in bins 3 through 6 for the qBus sample, *conditional* on the probability of being in at least one of those four bins. Thus we define $\hat{p}_{kj} = \hat{p}_{kj}^* / (\hat{p}_{3j}^* + \hat{p}_{4j}^* + \hat{p}_{5j}^* + \hat{p}_{6j}^*)$.³⁵

When we allow for potentially very different joint distributions of the explanatory variables Z_i and Z_j for the engagement-intensity model in the qBus and eBird samples, it is readily apparent that we should not use simply the differing observed *proportions* of people in each bin in the two samples to construct weights to be used in estimating the outcome

³⁵An alternative would be to attempt to fit a four-level ordered probit for only the qBus respondents, but there are relatively few eBird members in the qBus sample.

model. Our preferred approach would be more akin to the common method of constructing *exogenous* weights based on age brackets or gender. We wish to allow multiple exogenous factors to affect *expected* levels of engagement intensity for each eBird respondent. Consequently, we weight each observation in the eBird sample by $\hat{p}_{kj}/\hat{q}_{kj}$, $k = 3, \dots, 6$, normalized so that these weights sum to the sample size for the eBird sample. Use of these fitted probabilities recruits all of the exogenous or predetermined factors that capture heterogeneity in response propensities (i.e. the Z_i and Z_j data) to build the empirical weights, rather than just 0/1 group membership indicators.

E Additional complications to estimating IMR: Dealing with missing values for Z_j variables in the eBird sample

E.1 qBus sociodemographic variables have few missing values

Any empirical application of this methodology may have to confront the problem of what to do when there are missing values of some variables in one sample or the other. If the correction is based upon the standard sociodemographic variables available for qBus panel members, the data for those variables can be expected to be relatively complete. Any missing values in the qBus sample might be expected to be missing at random.

If other key variables intended to serve as regressors, Z_i , used in our weighting strategy, are drawn from survey questions posed to qBus participants, it is entirely possible that there may be item non-response for some of those variables. Such is the case in the present study, where our own questions produced the data for the number of days per year on which the respondent traveled more than one mile to see birds. Our own questions also elicited the data for participation in the Christmas Bird count and whether the individual also hunts birds, but we assume in the case of these latter two variables that the few missing responses are equivalent to “no”.

E.2 eBird sociodemographics match Census, but have more missing values

Missing values in the citizen-science eBird sample, for the sociodemographic variables that conform to the set available the qBus sample, are likely to be more of a problem. For example, due to time constraints for our survey of eBird members, we elected not to ask about individuals’ political ideologies. Had we anticipated being able to employ qBus questions to build sampling weights and estimated response propensities, it would have been prudent to be sure that the citizen science members were asked *every* standard sociodemographic question, verbatim, that is available with the qBus responses.

For this first example of our procedure, we can assemble conformable measures for gender, race, ethnicity, broad income brackets, four regions of the U.S., employment status and educational attainment. Some aggregation of categories has been required in each sample to produce matching categories. In future applications of this method, it would be prudent to minimize this type of aggregation. In the eBird data, we used categories that matched the U.S. Census, which would facilitate more-conventional comparisons of marginal distributions in the eBird sample to marginal distributions in the general population. However, the U.S. Census does not provide any information about engagement in citizen science, so our special-purpose qBus general-population sample is much superior in that way.

E.3 Using maximal available Z_j regressors for each eBird observation

Suppose there were no data in the eBird sample on any of the same sociodemographic regressors, Z_i provided by the qBus sample. There would still be valuable information in the qBus sample that could help construct either probability weights or propensity corrections. If one runs an ordered probit model to explain the engagement outcome in the eBird data, but use *no* explanatory variables, the result is a set of estimates for only the three cut-points between the four outcome levels in that eBird data. If one then calculates the predicted probabilities for each of the four participation intensities, the means of these probabilities, across the sample, match the proportions of the sample observed at each level.³⁶

E.4 If there are no Z_j regressors available for some eBird respondents

If there were no Z_j regressors available for some (small) subset of observations in the eBird sample, the best available option for weighting the observations at each level of participation intensity would be derived solely from (a) the predicted probabilities for each of the four relevant participation-intensity levels in the qBus sample (also estimated without regressors) relative to (b) the analogous predicted probabilities for the same four participation intensity levels in the qBus sample. The implicit model being used to predict participation intensities, in that case, would have no Z regressors, so there would be no basis for observable systematic heterogeneity in these probabilities. The weights would then differ only across the four observed participation intensity levels, but would be the same for every person who had no available Z variables in the eBird sample.

E.5 If only some subset of Z_j regressors is available for some eBird respondents

The most-general approach to weighting by participation intensity level or correcting parameters for different-from-average participation intensity would exploit the maximum information available in both samples, on an observation-by-observation basis for the eBird sample. To simplify, assume that only three basic factors are available as explanatory variables. In practice, each factor may be captured by a set of indicators for the categories of that factor, but we will assume for now that there is one continuous variable per factor such that the universe of potential Z variables consists of Z_1 , Z_2 , and Z_3 . All three variables (standing in for groups of indicator variables) are available for each qBus observation, but different

³⁶For binary probit and logit models, the means of the fitted probabilities will be either extremely close to the observed proportions, or exactly equal to those proportions, as can be proven by the algebra of the first-order conditions for the maximum likelihood estimation algorithm.

Table A3: Ordered-probit engagement-level models with minimum heterogeneity required to accommodate entire eBird sample: estimated using qBus sample, full eBird sample. Region variable is “West” for all eBird respondents.

	Ordered probit qBus data		Ordered probit eBird data	
Has participated in CBC	2.202***	(0.0670)	0.487***	(0.0678)
Hunts birds	0.526***	(0.0504)	0.0400	(0.128)
Region: Northeast	0.170**	(0.0697)	- ^a	
Region: Midwest	-0.0668	(0.0713)	- ^a	
Region: South	-0.0335	(0.0623)	- ^a	
cut1	1.271***	(0.0525)	-0.0249	(0.0527)
cut2	1.814***	(0.0575)	0.715***	(0.0552)
cut3	2.136***	(0.0622)	1.320***	(0.0623)
cut4	2.527***	(0.0687)	- ^b	
cut5	3.142***	(0.0819)	- ^b	
Observations	4161		1081	
Max. log-likelihood	-2591.22		-1396.30	

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$ ^aVar = 0 for all. ^bOnly 4 levels.

observations in the eBird sample have missing values for either one, two, or all three of these variables.

To fully exploit the available information, it is necessary to estimate an array of models for the qBus sample so that one of these models will be appropriate to transfer to every observation in the eBird sample. Suppose that we have indicators for the presence or absence of values for each of these three Z variables in the eBird sample. The number of necessary models using the qBus data could then be calculated using the sum of all the relevant combinations:

$$C_0^3 + C_1^3 + C_2^3 + C_3^3 = 1 + 3 + 3 + 1 = 8 \quad (7)$$

Of course, as the number of potential factors increases, the number of potentially relevant models to explain participation intensities in the qBus data can increase dramatically. In this study, we have six different factors with complete data in the qBus sample but missing data for at least some observations in the eBird sample: gender, age, income, region, employment status, and education. The number of potentially relevant models could be 64, but due to the correlation between missing values for some of these factors, the actual number of models required is only 30 in this study.

F Six-level ordered-probit eBird engagement-level models for all relevant subsets of regressors (using data from the qBus Sample); needed to compute weights, as well as to predict IMRs for eBird member survey sample

Table A4: qBus sample: Model 1-3 (of 30) to accommodate eBird missing values

	Model 1	Model 2	Model 3
Engagement-level indicator			
Has participated in CBC	2.202*** (0.0670)	2.144*** (0.0679)	2.120*** (0.0682)
Hunts birds	0.526*** (0.0504)	0.520*** (0.0509)	0.526*** (0.0514)
Region: Northeast	0.170** (0.0697)	0.162** (0.0705)	0.145** (0.0707)
Region: Midwest	-0.0668 (0.0713)	-0.0596 (0.0721)	-0.0580 (0.0722)
Region: South	-0.0335 (0.0623)	-0.0190 (0.0631)	-0.0135 (0.0633)
Empl. status: Part time		0.0240 (0.0674)	0.0508 (0.0684)
Empl. status: Looking for work		-0.133 (0.101)	-0.106 (0.102)
Empl. status: Unemployed		-0.151** (0.0711)	-0.120 (0.0737)
Empl. status: Retired		-0.632*** (0.0800)	-0.638*** (0.0805)
Education: High school			0.0424 (0.0688)
Education: Some college			-0.102 (0.0628)
Education: Masters degree			0.244*** (0.0784)
Education: Doctoral degree			0.209* (0.118)

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Table A4 – continued from previous page

cut1	1.271*** (0.0525)	1.150*** (0.0581)	1.171*** (0.0682)
cut2	1.814*** (0.0575)	1.704*** (0.0626)	1.728*** (0.0722)
cut3	2.136*** (0.0622)	2.032*** (0.0670)	2.061*** (0.0762)
cut4	2.527*** (0.0687)	2.431*** (0.0729)	2.465*** (0.0816)
cut5	3.142*** (0.0819)	3.054*** (0.0852)	3.096*** (0.0931)
Observations	4161	4161	4161
Max. log-likelihood	-2591.22	-2553.34	-2541.62
\bar{t} in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A5: qBus sample: Model 4-6 (of 30) to accommodate eBird missing values

	Model 4	Model 5	Model 6
Engagement-level indicator			
Has participated in CBC	2.023*** (0.0691)	2.166*** (0.0676)	2.132*** (0.0680)
Hunts birds	0.508*** (0.0522)	0.535*** (0.0510)	0.520*** (0.0509)
Age: 24 years or less	0.534*** (0.0964)		
Age: 25 to 34 years	0.560*** (0.0847)		
Age: 35 to 44 years	0.389*** (0.0873)		
Age: 55 to 64 years	-0.239** (0.107)		
Age: 65 years and up	-0.328** (0.131)		
Region: Northeast	0.162** (0.0718)	0.158** (0.0701)	0.166** (0.0706)
Region: Midwest	-0.0513 (0.0735)	-0.0621 (0.0714)	-0.0517 (0.0721)
Region: South	0.00627 (0.0643)	-0.0248 (0.0625)	-0.0109 (0.0632)
Empl. status: Part time	0.00864 (0.0719)		0.0495 (0.0681)
Empl. status: Looking for work	-0.194* (0.104)		-0.110 (0.101)
Empl. status: Unemployed	-0.166** (0.0755)		-0.112 (0.0725)
Empl. status: Retired	-0.138 (0.104)		-0.633*** (0.0799)
Education: High school	-0.0213 (0.0709)	0.0227 (0.0663)	
Education: Some college	-0.144** (0.0644)	-0.105* (0.0617)	
Education: Masters degree	0.269***	0.208***	

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Table A5 – continued from previous page

	(0.0798)	(0.0775)	
Education: Doctoral degree	0.204* (0.119)	0.162 (0.116)	
Gender: Female		-0.0946** (0.0472)	-0.135*** (0.0484)
cut1	1.441*** (0.0967)	1.226*** (0.0680)	1.097*** (0.0609)
cut2	2.021*** (0.100)	1.772*** (0.0720)	1.652*** (0.0652)
cut3	2.365*** (0.103)	2.098*** (0.0758)	1.981*** (0.0694)
cut4	2.780*** (0.108)	2.495*** (0.0812)	2.382*** (0.0750)
cut5	3.421*** (0.118)	3.120*** (0.0928)	3.007*** (0.0868)
Observations	4161	4161	4161
Max. log-likelihood	-2477.40	-2578.51	-2549.44
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A6: qBus sample: Model 7-9 (of 30) to accommodate eBird missing values

	Model 7	Model 8	Model 9
Engagement-level indicator			
Has participated in CBC	2.111*** (0.0683)	2.050*** (0.0685)	2.015*** (0.0689)
Hunts birds	0.525*** (0.0514)	0.488*** (0.0516)	0.505*** (0.0522)
Gender: Female	-0.116** (0.0487)	-0.212*** (0.0484)	-0.188*** (0.0488)
Region: Northeast	0.149** (0.0708)	0.187*** (0.0716)	0.168** (0.0719)
Region: Midwest	-0.0513 (0.0723)	-0.0368 (0.0733)	-0.0382 (0.0735)
Region: South	-0.00677 (0.0633)	0.0173 (0.0641)	0.0193 (0.0643)
Empl. status: Part time	0.0715 (0.0690)		
Empl. status: Looking for work	-0.0876 (0.102)		
Empl. status: Unemployed	-0.0878 (0.0749)		
Empl. status: Retired	-0.638*** (0.0805)		
Education: High school	0.0415 (0.0688)		-0.0593 (0.0690)
Education: Some college	-0.0957 (0.0629)		-0.149** (0.0638)
Education: Masters degree	0.239*** (0.0784)		0.266*** (0.0799)
Education: Doctoral degree	0.190 (0.118)		0.176 (0.120)
Age: 24 years or less		0.492*** (0.0926)	0.542*** (0.0937)
Age: 25 to 34 years		0.574*** (0.0837)	0.578*** (0.0841)
Age: 35 to 44 years		0.407***	0.399***

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Table A6 – continued from previous page

		(0.0866)	(0.0870)
Age: 55 to 64 years		-0.270*** (0.105)	-0.269** (0.105)
Age: 65 years and up		-0.375*** (0.113)	-0.422*** (0.114)
cut1	1.125*** (0.0707)	1.404*** (0.0894)	1.390*** (0.0980)
cut2	1.683*** (0.0746)	1.979*** (0.0929)	1.970*** (0.101)
cut3	2.016*** (0.0784)	2.320*** (0.0963)	2.316*** (0.104)
cut4	2.422*** (0.0835)	2.730*** (0.101)	2.733*** (0.109)
cut5	3.055*** (0.0947)	3.362*** (0.111)	3.375*** (0.119)
Observations	4161	4161	4161
Max. log-likelihood	-2538.76	-2489.65	-2474.54
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A7: qBus sample: Model 10-12 (of 30) to accommodate eBird missing values

	Model 10	Model 11	Model 12
Engagement-level indicator			
Has participated in CBC	2.034*** (0.0690)	2.006*** (0.0693)	2.016*** (0.0691)
Hunts birds	0.495*** (0.0517)	0.507*** (0.0522)	0.505*** (0.0522)
Gender: Female	-0.192*** (0.0494)	-0.176*** (0.0497)	-0.184*** (0.0492)
Age: 24 years or less	0.510*** (0.0959)	0.543*** (0.0966)	0.551*** (0.0947)
Age: 25 to 34 years	0.569*** (0.0846)	0.572*** (0.0849)	0.581*** (0.0846)
Age: 35 to 44 years	0.400*** (0.0871)	0.392*** (0.0875)	0.399*** (0.0870)
Age: 55 to 64 years	-0.251** (0.107)	-0.252** (0.107)	-0.271*** (0.105)
Age: 65 years and up	-0.307** (0.130)	-0.361*** (0.132)	-0.426*** (0.114)
Region: Northeast	0.187*** (0.0717)	0.168** (0.0720)	0.171** (0.0720)
Region: Midwest	-0.0398 (0.0734)	-0.0396 (0.0736)	-0.0349 (0.0736)
Region: South	0.0146 (0.0643)	0.0183 (0.0645)	0.0225 (0.0645)
Empl. status: Part time	0.00659 (0.0719)	0.0390 (0.0727)	
Empl. status: Looking for work	-0.204** (0.104)	-0.169 (0.105)	
Empl. status: Unemployed	-0.162** (0.0744)	-0.121 (0.0767)	
Empl. status: Retired	-0.143 (0.103)	-0.116 (0.104)	
Education: High school		-0.0276 (0.0710)	-0.0472 (0.0731)
Education: Some college		-0.138**	-0.147**

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Table A7 – continued from previous page

		(0.0645)	(0.0654)
Education: Masters degree	0.263***	(0.0799)	0.270*** (0.0810)
Education: Doctoral degree	0.175	(0.120)	0.178 (0.122)
Income: Less than 25K			-0.0820 (0.0815)
Income: 25 K to 50 K			-0.0137 (0.0755)
Income: 75 K to 100 K			-0.0489 (0.0845)
Income: 100 K or more			-0.0310 (0.0762)
<hr/>			
cut1	1.367*** (0.0908)	1.373*** (0.0985)	1.367*** (0.109)
cut2	1.943*** (0.0942)	1.954*** (0.102)	1.948*** (0.112)
cut3	2.284*** (0.0975)	2.300*** (0.105)	2.293*** (0.115)
cut4	2.696*** (0.102)	2.718*** (0.110)	2.711*** (0.119)
cut5	3.331*** (0.112)	3.362*** (0.119)	3.352*** (0.129)
Observations	4161	4161	4161
Max. log-likelihood	-2484.82	-2471.15	-2473.89
<hr/>			
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			
<hr/>			

Table A8: qBus sample: Model 13-15 (of 30) to accommodate eBird missing values

	Model 13	Model 14	Model 15
Engagement-level indicator			
Has participated in CBC	2.032*** (0.0691)	2.008*** (0.0694)	2.075*** (0.0685)
Hunts birds	0.500*** (0.0518)	0.506*** (0.0523)	0.0780 (0.0941)
Gender: Female	-0.186*** (0.0496)	-0.175*** (0.0499)	
Age: 24 years or less	0.526*** (0.0966)	0.545*** (0.0971)	
Age: 25 to 34 years	0.582*** (0.0850)	0.572*** (0.0854)	
Age: 35 to 44 years	0.399*** (0.0871)	0.393*** (0.0875)	
Age: 55 to 64 years	-0.258** (0.107)	-0.254** (0.107)	
Age: 65 years and up	-0.322** (0.130)	-0.366*** (0.132)	
Income: Less than 25K	-0.0569 (0.0826)	-0.0542 (0.0840)	
Income: 25 K to 50 K	-0.0201 (0.0755)	-0.0107 (0.0758)	
Income: 75 K to 100 K	-0.00868 (0.0838)	-0.0514 (0.0846)	
Income: 100 K or more	0.0624 (0.0729)	-0.0345 (0.0763)	
Region: Northeast	0.188*** (0.0718)	0.170** (0.0721)	0.158** (0.0715)
Region: Midwest	-0.0409 (0.0736)	-0.0363 (0.0738)	-0.0540 (0.0731)
Region: South	0.0182 (0.0644)	0.0203 (0.0647)	0.000262 (0.0638)
Empl. status: Part time	0.0255 (0.0734)	0.0431 (0.0737)	
Empl. status: Looking for work	-0.178*	-0.163	

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Table A8 – continued from previous page

	(0.106)	(0.106)	
Empl. status: Unemployed	-0.135*	-0.112	
	(0.0778)	(0.0790)	
Empl. status: Retired	-0.122	-0.114	
	(0.104)	(0.105)	
Education: High school		-0.0267	
		(0.0740)	
Education: Some college		-0.141**	
		(0.0658)	
Education: Masters degree		0.269***	
		(0.0810)	
Education: Doctoral degree		0.178	
		(0.122)	
Travel 1+ mile data available			0.354
			(0.688)
Trips 1+ miles = 0			-1.072
			(0.693)
Trips 1+ miles = [1,4)			-0.674
			(0.703)
Trips 1+ miles = [4,7)			-0.892
			(0.707)
Trips 1+ miles = [7,10)			-0.600
			(0.705)
Trips 1+ miles = [10,21)			-0.309
			(0.693)
Trips 1+ miles = [21,41)			-0.284
			(0.695)
Trips 1+ miles = [41,72)			0.0561
			(0.692)
Trips 1+ miles = [72,124)			0.293
			(0.690)
Trips 1+ miles = [124,174)			0.212
			(0.689)
Trips 1+ miles = [174,238)			0.341
			Continued on next page

Table A8 – continued from previous page

			(0.689)
Trips 1+ miles = [238,364)			0.634 (0.689)
Trips 1+ miles = 365			0.579 (0.714)
/			
cut1	1.386*** (0.102)	1.349*** (0.110)	1.188*** (0.0558)
cut2	1.963*** (0.105)	1.930*** (0.113)	1.769*** (0.0610)
cut3	2.304*** (0.108)	2.276*** (0.115)	2.112*** (0.0658)
cut4	2.718*** (0.113)	2.694*** (0.120)	2.518*** (0.0722)
cut5	3.354*** (0.122)	3.337*** (0.129)	3.143*** (0.0849)
Observations	4161	4161	4161
Max. log-likelihood	-2483.54	-2470.79	-2490.38
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A9: qBus sample: Model 16-18 (of 30) to accommodate eBird missing values

	Model 16	Model 17	Model 18
Engagement-level indicator			
Travel 1+ mile data available	0.299 (0.674)	0.242 (0.673)	0.183 (0.689)
Trips 1+ miles = 0	-1.017 (0.679)	-0.963 (0.678)	-0.921 (0.694)
Trips 1+ miles = [1,4)	-0.625 (0.689)	-0.485 (0.688)	-0.313 (0.705)
Trips 1+ miles = [4,7)	-0.852 (0.693)	-0.787 (0.693)	-0.590 (0.709)
Trips 1+ miles = [7,10)	-0.551 (0.691)	-0.528 (0.691)	-0.442 (0.708)
Trips 1+ miles = [10,21)	-0.264 (0.679)	-0.207 (0.678)	-0.105 (0.694)
Trips 1+ miles = [21,41)	-0.240 (0.681)	-0.144 (0.679)	-0.0796 (0.696)
Trips 1+ miles = [41,72)	0.0970 (0.678)	0.132 (0.676)	0.229 (0.692)
Trips 1+ miles = [72,124)	0.356 (0.676)	0.415 (0.674)	0.461 (0.690)
Trips 1+ miles = [124,174)	0.272 (0.675)	0.295 (0.674)	0.335 (0.690)
Trips 1+ miles = [174,238)	0.382 (0.675)	0.441 (0.673)	0.451 (0.689)
Trips 1+ miles = [238,364)	0.666 (0.674)	0.711 (0.673)	0.703 (0.689)
Trips 1+ miles = 365	0.623 (0.700)	0.630 (0.698)	0.649 (0.714)
Has participated in CBC	2.049*** (0.0689)	2.003*** (0.0696)	1.959*** (0.0699)
Hunts birds	0.0977 (0.0943)	0.0874 (0.0949)	0.0524 (0.0962)
Region: Northeast	0.143** (0.0718)	0.137* (0.0725)	0.175** (0.0731)
Region: Midwest	-0.0537	-0.0401	-0.0356

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Table A9 – continued from previous page

	(0.0733)	(0.0740)	(0.0749)
Region: South	0.00426 (0.0640)	0.0225 (0.0647)	0.0340 (0.0654)
Education: High school	-0.00150 (0.0677)	0.0284 (0.0702)	
Education: Some college	-0.103 (0.0631)	-0.0925 (0.0643)	
Education: Masters degree	0.222*** (0.0792)	0.250*** (0.0801)	
Education: Doctoral degree	0.176 (0.119)	0.205* (0.120)	
Empl. status: Part time		0.0552 (0.0698)	-0.0301 (0.0725)
Empl. status: Looking for work		-0.127 (0.105)	-0.246** (0.105)
Empl. status: Unemployed		-0.116 (0.0752)	-0.212*** (0.0747)
Empl. status: Retired		-0.612*** (0.0832)	-0.209** (0.105)
Age: 24 years or less			0.491*** (0.0977)
Age: 25 to 34 years			0.526*** (0.0861)
Age: 35 to 44 years			0.364*** (0.0888)
Age: 55 to 64 years			-0.186* (0.109)
Age: 65 years and up			-0.198 (0.131)
cut1	1.185*** (0.0684)	1.096*** (0.0717)	1.354*** (0.0917)
cut2	1.769*** (0.0728)	1.691*** (0.0759)	1.963*** (0.0954)
cut3	2.115*** (0.0770)	2.043*** (0.0800)	2.319*** (0.0989)
Continued on next page			

Table A9 – continued from previous page

cut4	2.527*** (0.0826)	2.463*** (0.0853)	2.741*** (0.104)
cut5	3.160*** (0.0941)	3.104*** (0.0964)	3.381*** (0.113)
Observations	4161	4161	4161
Max. log-likelihood	-2480.49	-2446.81	-2410.56
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A10: qBus sample: Model 19-21 (of 30) to accommodate eBird missing values

	Model 19	Model 20	Model 21
Engagement-level indicator			
Travel 1+ mile data available	0.127 (0.671)	0.166 (0.666)	0.146 (0.670)
Trips 1+ miles = 0	-0.867 (0.677)	-0.905 (0.672)	-0.885 (0.676)
Trips 1+ miles = [1,4)	-0.261 (0.688)	-0.295 (0.683)	-0.276 (0.686)
Trips 1+ miles = [4,7)	-0.549 (0.692)	-0.577 (0.687)	-0.569 (0.691)
Trips 1+ miles = [7,10)	-0.396 (0.691)	-0.408 (0.685)	-0.414 (0.690)
Trips 1+ miles = [10,21)	-0.0601 (0.677)	-0.0922 (0.672)	-0.0801 (0.676)
Trips 1+ miles = [21,41)	-0.0278 (0.678)	-0.0705 (0.673)	-0.0441 (0.677)
Trips 1+ miles = [41,72)	0.275 (0.675)	0.243 (0.670)	0.260 (0.673)
Trips 1+ miles = [72,124)	0.527 (0.673)	0.494 (0.668)	0.510 (0.672)
Trips 1+ miles = [124,174)	0.397 (0.673)	0.363 (0.667)	0.381 (0.671)
Trips 1+ miles = [174,238)	0.489 (0.672)	0.447 (0.667)	0.470 (0.671)
Trips 1+ miles = [238,364)	0.731 (0.671)	0.690 (0.666)	0.711 (0.670)
Trips 1+ miles = 365	0.697 (0.697)	0.688 (0.692)	0.685 (0.696)
Has participated in CBC	1.929*** (0.0703)	1.943*** (0.0700)	1.930*** (0.0704)
Hunts birds	0.0730 (0.0964)	0.0678 (0.0963)	0.0728 (0.0964)
Age: 24 years or less	0.527*** (0.0984)	0.534*** (0.0964)	0.534*** (0.0989)

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Table A10 – continued from previous page

Age: 25 to 34 years	0.530*** (0.0864)	0.545*** (0.0861)	0.536*** (0.0869)
Age: 35 to 44 years	0.358*** (0.0892)	0.365*** (0.0887)	0.358*** (0.0892)
Age: 55 to 64 years	-0.192* (0.110)	-0.226** (0.107)	-0.196* (0.110)
Age: 65 years and up	-0.262** (0.133)	-0.358*** (0.117)	-0.269** (0.134)
Region: Northeast	0.156** (0.0734)	0.160** (0.0734)	0.159** (0.0735)
Region: Midwest	-0.0333 (0.0751)	-0.0303 (0.0752)	-0.0306 (0.0753)
Region: South	0.0398 (0.0656)	0.0453 (0.0657)	0.0441 (0.0659)
Empl. status: Part time	0.00414 (0.0733)		0.0151 (0.0745)
Empl. status: Looking for work	-0.207* (0.106)		-0.193* (0.108)
Empl. status: Unemployed	-0.165** (0.0770)		-0.148* (0.0794)
Empl. status: Retired	-0.177* (0.106)		-0.167 (0.107)
Education: High school	-0.0321 (0.0722)	-0.0444 (0.0743)	-0.0177 (0.0752)
Education: Some college	-0.137** (0.0657)	-0.140** (0.0667)	-0.130* (0.0671)
Education: Masters degree	0.275*** (0.0812)	0.274*** (0.0824)	0.273*** (0.0824)
Education: Doctoral degree	0.201* (0.122)	0.189 (0.124)	0.191 (0.124)
Income: Less than 25K		-0.111 (0.0825)	-0.0713 (0.0851)
Income: 25 K to 50 K		-0.0287 (0.0770)	-0.0229 (0.0773)
Income: 75 K to 100 K		-0.0328	-0.0362

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Table A10 – continued from previous page

		(0.0865)	(0.0866)
Income: 100 K or more		0.00665 (0.0779)	0.0000751 (0.0781)
/			
cut1	1.357*** (0.0997)	1.380*** (0.110)	1.349*** (0.111)
cut2	1.970*** (0.103)	1.993*** (0.113)	1.963*** (0.114)
cut3	2.332*** (0.107)	2.355*** (0.116)	2.324*** (0.117)
cut4	2.761*** (0.111)	2.782*** (0.121)	2.754*** (0.122)
cut5	3.409*** (0.121)	3.428*** (0.130)	3.402*** (0.131)
Observations	4161	4161	4161
Max. log-likelihood	-2396.30	-2400.01	-2395.83
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A11: qBus sample: Model 22-24 (of 30) to accommodate eBird missing values

	Model 22	Model 23	Model 24
Engagement-level indicator			
Travel 1+ mile data available	0.343 (0.679)	0.295 (0.668)	0.241 (0.666)
Trips 1+ miles = 0	-1.062 (0.685)	-1.013 (0.674)	-0.958 (0.671)
Trips 1+ miles = [1,4)	-0.664 (0.694)	-0.621 (0.684)	-0.481 (0.681)
Trips 1+ miles = [4,7)	-0.885 (0.698)	-0.850 (0.687)	-0.787 (0.686)
Trips 1+ miles = [7,10)	-0.580 (0.697)	-0.539 (0.686)	-0.517 (0.684)
Trips 1+ miles = [10,21)	-0.289 (0.685)	-0.251 (0.674)	-0.196 (0.671)
Trips 1+ miles = [21,41)	-0.264 (0.686)	-0.228 (0.675)	-0.132 (0.673)
Trips 1+ miles = [41,72)	0.0791 (0.683)	0.112 (0.672)	0.146 (0.669)
Trips 1+ miles = [72,124)	0.303 (0.681)	0.358 (0.670)	0.415 (0.667)
Trips 1+ miles = [124,174)	0.231 (0.681)	0.283 (0.670)	0.305 (0.667)
Trips 1+ miles = [174,238)	0.357 (0.680)	0.391 (0.669)	0.448 (0.667)
Trips 1+ miles = [238,364)	0.649 (0.680)	0.675 (0.669)	0.720 (0.666)
Trips 1+ miles = 365	0.590 (0.705)	0.629 (0.695)	0.634 (0.692)
Has participated in CBC	2.060*** (0.0688)	2.038*** (0.0691)	1.994*** (0.0697)
Hunts birds	0.0756 (0.0940)	0.0937 (0.0943)	0.0816 (0.0949)
Gender: Female	-0.128*** (0.0478)	-0.104** (0.0484)	-0.120** (0.0498)

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Table A11 – continued from previous page

Region: Northeast	0.162** (0.0716)	0.147** (0.0719)	0.141* (0.0726)
Region: Midwest	-0.0460 (0.0732)	-0.0472 (0.0733)	-0.0326 (0.0741)
Region: South	0.00866 (0.0639)	0.0109 (0.0640)	0.0300 (0.0648)
Education: High school		0.00516 (0.0679)	0.0277 (0.0703)
Education: Some college		-0.0931 (0.0632)	-0.0858 (0.0643)
Education: Masters degree		0.215*** (0.0793)	0.244*** (0.0801)
Education: Doctoral degree		0.156 (0.119)	0.184 (0.120)
Empl. status: Part time			0.0766 (0.0705)
Empl. status: Looking for work			-0.108 (0.105)
Empl. status: Unemployed			-0.0833 (0.0765)
Empl. status: Retired			-0.610*** (0.0831)
cut1	1.128*** (0.0599)	1.140*** (0.0714)	1.051*** (0.0740)
cut2	1.711*** (0.0647)	1.725*** (0.0756)	1.646*** (0.0781)
cut3	2.054*** (0.0691)	2.071*** (0.0796)	1.999*** (0.0820)
cut4	2.462*** (0.0751)	2.484*** (0.0849)	2.421*** (0.0871)
cut5	3.091*** (0.0872)	3.120*** (0.0960)	3.063*** (0.0979)
Observations	4161	4161	4161
Max. log-likelihood	-2486.77	-2478.16	-2443.92
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A12: qBus sample: Model 25-27 (of 30) to accommodate eBird missing values

	Model 25	Model 26	Model 27
Engagement-level indicator			
Travel 1+ mile data available	0.125 (0.659)	0.170 (0.676)	0.122 (0.662)
Trips 1+ miles = 0	-0.858 (0.665)	-0.904 (0.681)	-0.856 (0.668)
Trips 1+ miles = [1,4)	-0.250 (0.676)	-0.296 (0.692)	-0.249 (0.679)
Trips 1+ miles = [4,7)	-0.527 (0.681)	-0.571 (0.696)	-0.537 (0.683)
Trips 1+ miles = [7,10)	-0.350 (0.679)	-0.412 (0.695)	-0.373 (0.682)
Trips 1+ miles = [10,21)	-0.0324 (0.665)	-0.0784 (0.681)	-0.0411 (0.668)
Trips 1+ miles = [21,41)	-0.0168 (0.666)	-0.0510 (0.683)	-0.00610 (0.669)
Trips 1+ miles = [41,72)	0.300 (0.663)	0.260 (0.679)	0.300 (0.665)
Trips 1+ miles = [72,124)	0.533 (0.661)	0.471 (0.677)	0.531 (0.664)
Trips 1+ miles = [124,174)	0.412 (0.661)	0.359 (0.677)	0.413 (0.663)
Trips 1+ miles = [174,238)	0.495 (0.660)	0.469 (0.676)	0.501 (0.663)
Trips 1+ miles = [238,364)	0.741 (0.659)	0.724 (0.676)	0.745 (0.662)
Trips 1+ miles = 365	0.723 (0.686)	0.664 (0.702)	0.708 (0.688)
Has participated in CBC	1.923*** (0.0701)	1.941*** (0.0701)	1.913*** (0.0704)
Hunts birds	0.0591 (0.0963)	0.0436 (0.0963)	0.0642 (0.0965)
Gender: Female	-0.184*** (0.0498)	-0.187*** (0.0503)	-0.171*** (0.0507)

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Table A12 – continued from previous page

Age: 24 years or less	0.534*** (0.0957)	0.501*** (0.0980)	0.535*** (0.0987)
Age: 25 to 34 years	0.549*** (0.0857)	0.538*** (0.0863)	0.542*** (0.0866)
Age: 35 to 44 years	0.367*** (0.0889)	0.366*** (0.0890)	0.360*** (0.0894)
Age: 55 to 64 years	-0.232** (0.107)	-0.198* (0.110)	-0.204* (0.110)
Age: 65 years and up	-0.376*** (0.117)	-0.233* (0.132)	-0.292** (0.134)
Region: Northeast	0.162** (0.0734)	0.180** (0.0732)	0.162** (0.0735)
Region: Midwest	-0.0204 (0.0751)	-0.0222 (0.0750)	-0.0212 (0.0752)
Region: South	0.0522 (0.0656)	0.0478 (0.0656)	0.0520 (0.0658)
Education: High school	-0.0723 (0.0702)		-0.0377 (0.0723)
Education: Some college	-0.143** (0.0651)		-0.130** (0.0658)
Education: Masters degree	0.271*** (0.0813)		0.269*** (0.0814)
Education: Doctoral degree	0.170 (0.122)		0.170 (0.122)
Empl. status: Part time		0.00313 (0.0732)	0.0336 (0.0740)
Empl. status: Looking for work		-0.219** (0.106)	-0.183* (0.107)
Empl. status: Unemployed		-0.162** (0.0760)	-0.120 (0.0782)
Empl. status: Retired		-0.184* (0.105)	-0.154 (0.106)
cut1	1.311*** (0.101)	1.285*** (0.0934)	1.292*** (0.101)
cut2	1.926***	1.896***	1.908***

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Table A12 – continued from previous page

	(0.104)	(0.0971)	(0.105)
cut3	2.289*** (0.108)	2.254*** (0.100)	2.271*** (0.108)
cut4	2.719*** (0.112)	2.679*** (0.105)	2.703*** (0.113)
cut5	3.368*** (0.121)	3.322*** (0.114)	3.354*** (0.122)
Observations	4161	4161	4161
Max. log-likelihood	-2394.41	-2403.62	-2390.64
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A13: qBus sample: Model 28-30 (of 30) to accommodate eBird missing values

	Model 28	Model 29	Model 30
Engagement-level indicator			
Travel 1+ mile data available	0.192 (0.667)	0.148 (0.658)	0.174 (0.671)
Trips 1+ miles = 0	-0.929 (0.673)	-0.882 (0.664)	-0.912 (0.677)
Trips 1+ miles = [1,4)	-0.318 (0.684)	-0.269 (0.675)	-0.301 (0.688)
Trips 1+ miles = [4,7)	-0.579 (0.688)	-0.553 (0.680)	-0.576 (0.693)
Trips 1+ miles = [7,10)	-0.406 (0.687)	-0.376 (0.678)	-0.414 (0.691)
Trips 1+ miles = [10,21)	-0.0974 (0.673)	-0.0572 (0.664)	-0.0898 (0.677)
Trips 1+ miles = [21,41)	-0.0826 (0.674)	-0.0376 (0.665)	-0.0588 (0.678)
Trips 1+ miles = [41,72)	0.250 (0.671)	0.279 (0.662)	0.263 (0.675)
Trips 1+ miles = [72,124)	0.455 (0.669)	0.510 (0.660)	0.470 (0.673)
Trips 1+ miles = [124,174)	0.352 (0.669)	0.390 (0.660)	0.367 (0.673)
Trips 1+ miles = [174,238)	0.443 (0.668)	0.472 (0.659)	0.463 (0.672)
Trips 1+ miles = [238,364)	0.700 (0.667)	0.715 (0.658)	0.718 (0.671)
Trips 1+ miles = 365	0.667 (0.693)	0.707 (0.685)	0.665 (0.697)
Has participated in CBC	1.947*** (0.0700)	1.923*** (0.0703)	1.937*** (0.0703)
Hunts birds	0.0422 (0.0961)	0.0595 (0.0963)	0.0497 (0.0963)
Gender: Female	-0.189*** (0.0499)	-0.178*** (0.0502)	-0.178*** (0.0506)

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Table A13 – continued from previous page

Age: 24 years or less	0.523*** (0.0960)	0.547*** (0.0966)	0.521*** (0.0987)
Age: 25 to 34 years	0.566*** (0.0858)	0.556*** (0.0863)	0.554*** (0.0867)
Age: 35 to 44 years	0.372*** (0.0885)	0.367*** (0.0889)	0.365*** (0.0890)
Age: 55 to 64 years	-0.237** (0.107)	-0.235** (0.107)	-0.208* (0.110)
Age: 65 years and up	-0.334*** (0.115)	-0.379*** (0.117)	-0.253* (0.132)
Income: Less than 25K	-0.103 (0.0809)	-0.0873 (0.0829)	-0.0628 (0.0839)
Income: 25 K to 50 K	-0.0368 (0.0768)	-0.0224 (0.0771)	-0.0296 (0.0771)
Income: 75 K to 100 K	0.00562 (0.0858)	-0.0399 (0.0866)	0.000688 (0.0859)
Income: 100 K or more	0.0929 (0.0746)	-0.00666 (0.0782)	0.0838 (0.0748)
Region: Northeast	0.184** (0.0732)	0.166** (0.0736)	0.182** (0.0734)
Region: Midwest	-0.0215 (0.0751)	-0.0177 (0.0753)	-0.0234 (0.0752)
Region: South	0.0557 (0.0656)	0.0566 (0.0658)	0.0525 (0.0658)
Education: High school		-0.0511 (0.0745)	
Education: Some college		-0.134** (0.0668)	
Education: Masters degree		0.270*** (0.0825)	
Education: Doctoral degree		0.162 (0.124)	
Empl. status: Part time			0.0268 (0.0748)
Empl. status: Looking for work			-0.188*

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Table A13 – continued from previous page

			(0.108)
Empl. status: Unemployed			-0.129 (0.0795)
Empl. status: Retired			-0.155 (0.106)
cut1	1.345*** (0.104)	1.299*** (0.112)	1.313*** (0.105)
cut2	1.956*** (0.107)	1.914*** (0.115)	1.925*** (0.108)
cut3	2.315*** (0.110)	2.277*** (0.118)	2.284*** (0.111)
cut4	2.740*** (0.115)	2.708*** (0.123)	2.711*** (0.116)
cut5	3.383*** (0.124)	3.357*** (0.132)	3.356*** (0.125)
Observations	4161	4161	4161
Max. log-likelihood	-2405.49	-2393.71	-2401.66
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

G Four-level ordered-probit eBird engagement-level models for all relevant subsets of regressors (using data from the eBird member survey sample); needed to compute weights

Table A14: eBird sample: Model 1-3 (of 30) to accommodate missing values

	Model 1	Model 2	Model 3
Engagement-level indicator			
Has participated in CBC	0.487*** (0.0678)	0.556*** (0.0744)	0.525*** (0.0759)
Hunts birds	0.0400 (0.128)	-0.0868 (0.139)	-0.0443 (0.140)
Empl. status: Part time		-0.255* (0.140)	-0.210 (0.143)
Empl. status: Looking for work		-0.587 (0.425)	-0.562 (0.428)
Empl. status: Unemployed		-0.154 (0.157)	-0.0841 (0.161)
Empl. status: Retired		-0.501*** (0.0807)	-0.480*** (0.0820)
Education: High school			0.197 (0.219)
Education: Some college			-0.183 (0.120)
Education: Masters degree			0.0652 (0.0905)
Education: Doctoral degree			0.266** (0.125)
cut1	-0.0249 (0.0527)	-0.294*** (0.0759)	-0.258*** (0.0967)
cut2	0.715*** (0.0552)	0.482*** (0.0762)	0.527*** (0.0972)
cut3	1.320*** (0.0623)	1.086*** (0.0818)	1.131*** (0.102)
Observations	1081	918	899
Max. log-likelihood	-1396.30	-1162.68	-1135.31
<i>t</i> in parentheses			

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Table A14 – continued from previous page

* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Table A15: eBird sample: Model 4-6 (of 30) to accommodate missing values

	Model 4	Model 5	Model 6
Engagement-level indicator			
Has participated in CBC	0.567*** (0.0769)	0.413*** (0.0700)	0.522*** (0.0749)
Hunts birds	-0.0758 (0.142)	-0.0716 (0.131)	-0.214 (0.141)
Age: 24 years or less	0.963*** (0.352)		
Age: 25 to 34 years	0.439** (0.172)		
Age: 35 to 44 years	0.330** (0.157)		
Age: 55 to 64 years	-0.140 (0.125)		
Age: 65 years and up	-0.163 (0.152)		
Empl. status: Part time	-0.222 (0.147)		-0.181 (0.141)
Empl. status: Looking for work	-0.693 (0.435)		-0.520 (0.425)
Empl. status: Unemployed	-0.0923 (0.164)		-0.0523 (0.159)
Empl. status: Retired	-0.260** (0.121)		-0.469*** (0.0812)
Education: High school	0.0937 (0.234)	0.102 (0.194)	
Education: Some college	-0.135 (0.122)	-0.159 (0.108)	
Education: Masters degree	0.126 (0.0919)	0.0479 (0.0833)	
Education: Doctoral degree	0.344*** (0.127)	0.227* (0.116)	
Gender: Female		-0.357*** (0.0717)	-0.373*** (0.0771)
/cut1	-0.141	-0.268***	-0.518***

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Table A15 – continued from previous page

	(0.126)	(0.0930)	(0.0889)
cut2	0.666*** (0.127)	0.498*** (0.0934)	0.272*** (0.0879)
cut3	1.276*** (0.131)	1.113*** (0.0968)	0.889*** (0.0918)
Observations	898	1053	916
Max. log-likelihood	-1121.46	-1344.47	-1149.42
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A16: eBird sample: Model 7-9 (of 30) to accommodate missing values

	Model 7	Model 8	Model 9
Engagement-level indicator			
Has participated in CBC	0.493*** (0.0765)	0.534*** (0.0700)	0.500*** (0.0715)
Hunts birds	-0.168 (0.143)	-0.208 (0.133)	-0.162 (0.133)
Gender: Female	-0.344*** (0.0787)	-0.412*** (0.0706)	-0.378*** (0.0724)
Empl. status: Part time	-0.144 (0.144)		
Empl. status: Looking for work	-0.503 (0.427)		
Empl. status: Unemployed	0.0109 (0.163)		
Empl. status: Retired	-0.452*** (0.0824)		
Education: High school	0.115 (0.220)		0.00592 (0.207)
Education: Some college	-0.200* (0.121)		-0.129 (0.110)
Education: Masters degree	0.0603 (0.0908)		0.166* (0.0852)
Education: Doctoral degree	0.198 (0.126)		0.336*** (0.118)
Age: 24 years or less		0.632** (0.255)	0.769*** (0.268)
Age: 25 to 34 years		0.328** (0.155)	0.389** (0.157)
Age: 35 to 44 years		0.172 (0.141)	0.187 (0.142)
Age: 55 to 64 years		-0.305*** (0.107)	-0.306*** (0.108)
Age: 65 years and up		-0.431*** (0.105)	-0.439*** (0.106)
/ cut1	-0.480***	-0.490***	-0.394***

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Table A16 – continued from previous page

	(0.110)	(0.107)	(0.124)
cut2	0.317*** (0.109)	0.305*** (0.106)	0.413*** (0.124)
cut3	0.931*** (0.112)	0.939*** (0.109)	1.046*** (0.127)
Observations	897	1071	1051
Max. log-likelihood	-1124.29	-1339.49	-1307.49
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A17: eBird sample: Model 10-12 (of 30) to accommodate missing values

	Model 10	Model 11	Model 12
Engagement-level indicator			
Has participated in CBC	0.568*** (0.0761)	0.535*** (0.0775)	0.491*** (0.0795)
Hunts birds	-0.259* (0.143)	-0.207 (0.144)	-0.186 (0.140)
Gender: Female	-0.385*** (0.0779)	-0.359*** (0.0796)	-0.364*** (0.0804)
Age: 24 years or less	0.875*** (0.334)	0.924*** (0.352)	0.789** (0.315)
Age: 25 to 34 years	0.391** (0.171)	0.424** (0.173)	0.317* (0.167)
Age: 35 to 44 years	0.317** (0.156)	0.321** (0.157)	0.125 (0.151)
Age: 55 to 64 years	-0.154 (0.124)	-0.161 (0.126)	-0.376*** (0.117)
Age: 65 years and up	-0.217 (0.151)	-0.232 (0.154)	-0.405*** (0.118)
Empl. status: Part time	-0.180 (0.147)	-0.136 (0.149)	
Empl. status: Looking for work	-0.663 (0.433)	-0.635 (0.435)	
Empl. status: Unemployed	-0.0534 (0.163)	0.00968 (0.165)	
Empl. status: Retired	-0.222* (0.120)	-0.188 (0.123)	
Education: High school		0.0161 (0.235)	0.145 (0.237)
Education: Some college		-0.149 (0.122)	-0.135 (0.122)
Education: Masters degree		0.125 (0.0922)	0.108 (0.0943)
Education: Doctoral degree		0.279** (0.128)	0.251* (0.133)
Income: Less than 25K			-0.133

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Table A17 – continued from previous page

			(0.170)
Income: 25 K to 50 K			0.118 (0.117)
Income: 75 K to 100 K			-0.127 (0.122)
Income: 100 K or more			0.117 (0.106)
cut1	-0.464*** (0.119)	-0.383*** (0.137)	-0.478*** (0.154)
cut2	0.347*** (0.118)	0.438*** (0.137)	0.378** (0.154)
cut3	0.972*** (0.122)	1.059*** (0.140)	1.017*** (0.156)
Observations	914	896	853
Max. log-likelihood	-1134.81	-1109.77	-1076.62
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A18: eBird sample: Model 13-15 (of 30) to accommodate missing values

	Model 13	Model 14	Model 15
Engagement-level indicator			
Has participated in CBC	0.562*** (0.0846)	0.534*** (0.0867)	0.0305 (0.0844)
Hunts birds	-0.290* (0.148)	-0.241 (0.150)	0.106 (0.152)
Gender: Female	-0.387*** (0.0867)	-0.375*** (0.0888)	
Age: 24 years or less	1.021*** (0.396)	0.986** (0.403)	
Age: 25 to 34 years	0.341* (0.185)	0.330* (0.188)	
Age: 35 to 44 years	0.233 (0.167)	0.229 (0.168)	
Age: 55 to 64 years	-0.195 (0.134)	-0.217 (0.136)	
Age: 65 years and up	-0.103 (0.167)	-0.125 (0.170)	
Income: Less than 25K	-0.267 (0.193)	-0.198 (0.200)	
Income: 25 K to 50 K	0.0989 (0.124)	0.150 (0.127)	
Income: 75 K to 100 K	-0.204 (0.131)	-0.182 (0.132)	
Income: 100 K or more	0.0531 (0.115)	0.0303 (0.117)	
Empl. status: Part time	-0.181 (0.160)	-0.164 (0.161)	
Empl. status: Looking for work	-0.476 (0.462)	-0.482 (0.465)	
Empl. status: Unemployed	-0.163 (0.188)	-0.127 (0.190)	
Empl. status: Retired	-0.343** (0.135)	-0.321** (0.136)	
Education: High school		0.130	

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Table A18 – continued from previous page

		(0.259)	
Education: Some college		-0.142 (0.138)	
Education: Masters degree		0.0764 (0.102)	
Education: Doctoral degree		0.196 (0.144)	
Travel 1+ mile data available		0 (.)	
Trips 1+ miles = 0		-2.765*** (0.187)	
Trips 1+ miles = [1,4)		-2.923*** (0.213)	
Trips 1+ miles = [4,7)		-1.944*** (0.222)	
Trips 1+ miles = [7,10)		-1.587*** (0.283)	
Trips 1+ miles = [10,21)		-1.556*** (0.202)	
Trips 1+ miles = [21,41)		-1.371*** (0.216)	
Trips 1+ miles = [41,72)		-1.097*** (0.207)	
Trips 1+ miles = [72,124)		-0.695*** (0.213)	
Trips 1+ miles = [124,174)		-0.560** (0.231)	
Trips 1+ miles = [174,238)		-0.426 (0.265)	
Trips 1+ miles = [238,364)		-0.399* (0.229)	
Trips 1+ miles = 365		0 (.)	
/			
cut1	-0.599***	-0.555***	-2.506***
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Table A18 – continued from previous page

	(0.156)	(0.174)	(0.187)
cut2	0.285* (0.156)	0.335* (0.173)	-1.346*** (0.178)
cut3	0.908*** (0.159)	0.954*** (0.176)	-0.401** (0.173)
Observations	740	727	831
Max. log-likelihood	-924.96	-907.59	-875.39
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A19: eBird sample: Model 16-18 (of 30) to accommodate missing values

	Model 16	Model 17	Model 18
Engagement-level indicator			
Travel 1+ mile data available	0 (.)	0 (.)	0 (.)
Trips 1+ miles = 0	-2.761*** (0.190)	-2.837*** (0.211)	-2.855*** (0.208)
Trips 1+ miles = [1,4)	-2.983*** (0.218)	-3.107*** (0.242)	-3.090*** (0.240)
Trips 1+ miles = [4,7)	-1.977*** (0.226)	-1.959*** (0.258)	-1.955*** (0.255)
Trips 1+ miles = [7,10)	-1.698*** (0.290)	-1.993*** (0.314)	-1.896*** (0.309)
Trips 1+ miles = [10,21)	-1.546*** (0.205)	-1.678*** (0.226)	-1.692*** (0.224)
Trips 1+ miles = [21,41)	-1.368*** (0.219)	-1.439*** (0.240)	-1.453*** (0.237)
Trips 1+ miles = [41,72)	-1.105*** (0.209)	-1.196*** (0.232)	-1.225*** (0.232)
Trips 1+ miles = [72,124)	-0.678*** (0.216)	-0.629*** (0.238)	-0.676*** (0.236)
Trips 1+ miles = [124,174)	-0.592** (0.235)	-0.629** (0.264)	-0.622** (0.261)
Trips 1+ miles = [174,238)	-0.404 (0.272)	-0.546* (0.291)	-0.568** (0.284)
Trips 1+ miles = [238,364)	-0.410* (0.234)	-0.522** (0.258)	-0.551** (0.255)
Trips 1+ miles = 365	0 (.)	0 (.)	0 (.)
Has participated in CBC	0.0272 (0.0859)	0.125 (0.0935)	0.160* (0.0936)
Hunts birds	0.108 (0.153)	0.00874 (0.170)	-0.00447 (0.170)
Education: High school	0.427* (0.235)	0.462* (0.255)	
Education: Some college	0.00506	-0.114	

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Table A19 – continued from previous page

	(0.134)	(0.150)	
Education: Masters degree	0.176* (0.0980)	0.183* (0.108)	
Education: Doctoral degree	0.147 (0.133)	0.0672 (0.144)	
Empl. status: Part time		-0.116 (0.169)	-0.226 (0.173)
Empl. status: Looking for work		-0.718 (0.587)	-0.976* (0.589)
Empl. status: Unemployed		0.0905 (0.186)	0.0520 (0.185)
Empl. status: Retired		-0.322*** (0.0976)	-0.342** (0.142)
Age: 24 years or less			0.755** (0.346)
Age: 25 to 34 years			0.206 (0.194)
Age: 35 to 44 years			0.281 (0.180)
Age: 55 to 64 years			-0.110 (0.145)
Age: 65 years and up			0.130 (0.178)
cut1	-2.420*** (0.202)	-2.670*** (0.231)	-2.711*** (0.235)
cut2	-1.243*** (0.193)	-1.434*** (0.221)	-1.457*** (0.225)
cut3	-0.303 (0.188)	-0.496** (0.215)	-0.510** (0.220)
Observations	810	693	707
Max. log-likelihood	-850.08	-711.03	-722.39
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A20: eBird sample: Model 19-21 (of 30) to accommodate missing values

	Model 19	Model 20	Model 21
Engagement-level indicator			
Travel 1+ mile data available	0 (.)	0 (.)	0 (.)
Trips 1+ miles = 0	-2.867*** (0.212)	-2.810*** (0.207)	-2.850*** (0.228)
Trips 1+ miles = [1,4)	-3.151*** (0.245)	-3.071*** (0.242)	-3.140*** (0.267)
Trips 1+ miles = [4,7)	-2.024*** (0.259)	-2.120*** (0.250)	-1.884*** (0.286)
Trips 1+ miles = [7,10)	-2.086*** (0.318)	-2.084*** (0.346)	-2.285*** (0.370)
Trips 1+ miles = [10,21)	-1.707*** (0.227)	-1.800*** (0.226)	-1.851*** (0.249)
Trips 1+ miles = [21,41)	-1.484*** (0.241)	-1.494*** (0.238)	-1.520*** (0.261)
Trips 1+ miles = [41,72)	-1.247*** (0.234)	-1.341*** (0.227)	-1.363*** (0.253)
Trips 1+ miles = [72,124)	-0.675*** (0.239)	-0.844*** (0.233)	-0.728*** (0.258)
Trips 1+ miles = [124,174)	-0.677** (0.265)	-0.696*** (0.258)	-0.654** (0.292)
Trips 1+ miles = [174,238)	-0.565* (0.292)	-0.465 (0.298)	-0.569* (0.321)
Trips 1+ miles = [238,364)	-0.575** (0.260)	-0.396 (0.260)	-0.424 (0.286)
Trips 1+ miles = 365	0 (.)	0 (.)	0 (.)
Has participated in CBC	0.150 (0.0948)	0.103 (0.0972)	0.183* (0.106)
Hunts birds	-0.0170 (0.171)	0.0233 (0.164)	-0.0400 (0.177)
Age: 24 years or less	0.640* (0.370)	0.902*** (0.334)	1.019** (0.423)
Age: 25 to 34 years	0.267	0.208	0.298

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Table A20 – continued from previous page

	(0.196)	(0.191)	(0.215)
Age: 35 to 44 years	0.301* (0.181)	0.308* (0.174)	0.325* (0.192)
Age: 55 to 64 years	-0.128 (0.148)	-0.300** (0.137)	-0.117 (0.159)
Age: 65 years and up	0.102 (0.181)	-0.184 (0.137)	0.161 (0.200)
Empl. status: Part time	-0.189 (0.175)		-0.169 (0.187)
Empl. status: Looking for work	-0.908 (0.593)		-0.825 (0.650)
Empl. status: Unemployed	0.0780 (0.189)		-0.0457 (0.214)
Empl. status: Retired	-0.307** (0.145)		-0.343** (0.162)
Education: High school	0.392 (0.275)	0.606** (0.280)	0.718** (0.308)
Education: Some college	-0.0874 (0.152)	0.0891 (0.150)	0.00245 (0.169)
Education: Masters degree	0.222** (0.110)	0.305*** (0.110)	0.259** (0.121)
Education: Doctoral degree	0.116 (0.147)	0.160 (0.150)	0.0245 (0.164)
Income: Less than 25K		0.0219 (0.209)	-0.0785 (0.254)
Income: 25 K to 50 K		0.154 (0.138)	0.154 (0.150)
Income: 75 K to 100 K		0.0584 (0.144)	0.00504 (0.157)
Income: 100 K or more		0.240* (0.123)	0.167 (0.136)
cut1	-2.632*** (0.250)	-2.483*** (0.249)	-2.586*** (0.282)
cut2	-1.370*** (0.240)	-1.211*** (0.241)	-1.246*** (0.273)
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Table A20 – continued from previous page

cut3	-0.425*	-0.241	-0.302
	(0.236)	(0.236)	(0.268)
Observations	692	674	573
Max. log-likelihood	-704.13	-697.49	-583.38

t in parentheses
 * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$

Table A21: eBird sample: Model 22-24 (of 30) to accommodate missing values

	Model 22	Model 23	Model 24
Engagement-level indicator			
Travel 1+ mile data available	0 (.)	0 (.)	0 (.)
Trips 1+ miles = 0	-2.735*** (0.188)	-2.732*** (0.191)	-2.810*** (0.211)
Trips 1+ miles = [1,4)	-2.886*** (0.214)	-2.952*** (0.219)	-3.082*** (0.243)
Trips 1+ miles = [4,7)	-1.922*** (0.223)	-1.956*** (0.226)	-1.933*** (0.258)
Trips 1+ miles = [7,10)	-1.545*** (0.284)	-1.659*** (0.291)	-1.948*** (0.315)
Trips 1+ miles = [10,21)	-1.514*** (0.203)	-1.512*** (0.206)	-1.650*** (0.227)
Trips 1+ miles = [21,41)	-1.334*** (0.217)	-1.341*** (0.220)	-1.416*** (0.240)
Trips 1+ miles = [41,72)	-1.089*** (0.206)	-1.098*** (0.209)	-1.189*** (0.232)
Trips 1+ miles = [72,124)	-0.668*** (0.213)	-0.658*** (0.216)	-0.611** (0.238)
Trips 1+ miles = [124,174)	-0.551** (0.231)	-0.581** (0.235)	-0.623** (0.265)
Trips 1+ miles = [174,238)	-0.429 (0.265)	-0.411 (0.272)	-0.563* (0.291)
Trips 1+ miles = [238,364)	-0.394* (0.229)	-0.410* (0.234)	-0.518** (0.258)
Trips 1+ miles = 365	0 (.)	0 (.)	0 (.)
Has participated in CBC	0.0210 (0.0848)	0.0183 (0.0862)	0.115 (0.0939)
Hunts birds	0.0512 (0.155)	0.0583 (0.156)	-0.0406 (0.172)
Gender: Female	-0.160* (0.0830)	-0.132 (0.0855)	-0.148 (0.0940)
Education: High school		0.404*	0.437*

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Table A21 – continued from previous page

		(0.235)	(0.255)
Education: Some college		0.00943 (0.134)	-0.114 (0.151)
Education: Masters degree		0.174* (0.0981)	0.183* (0.108)
Education: Doctoral degree		0.115 (0.135)	0.0368 (0.146)
Empl. status: Part time			-0.0868 (0.170)
Empl. status: Looking for work			-0.716 (0.584)
Empl. status: Unemployed			0.135 (0.188)
Empl. status: Retired			-0.305*** (0.0980)
cut1	-2.587*** (0.192)	-2.490*** (0.207)	-2.738*** (0.236)
cut2	-1.415*** (0.182)	-1.309*** (0.198)	-1.498*** (0.225)
cut3	-0.466*** (0.176)	-0.365* (0.193)	-0.557** (0.220)
Observations	826	808	691
Max. log-likelihood	-868.79	-847.83	-708.91
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A22: eBird sample: Model 25-27 (of 30) to accommodate missing values

	Model 25	Model 26	Model 27
Engagement-level indicator			
Travel 1+ mile data available	0 (.)	0 (.)	0 (.)
Trips 1+ miles = 0	-2.750*** (0.192)	-2.820*** (0.209)	-2.838*** (0.212)
Trips 1+ miles = [1,4)	-2.969*** (0.221)	-3.053*** (0.241)	-3.123*** (0.245)
Trips 1+ miles = [4,7)	-2.031*** (0.227)	-1.928*** (0.255)	-1.997*** (0.260)
Trips 1+ miles = [7,10)	-1.786*** (0.294)	-1.850*** (0.310)	-2.041*** (0.320)
Trips 1+ miles = [10,21)	-1.559*** (0.207)	-1.658*** (0.224)	-1.678*** (0.228)
Trips 1+ miles = [21,41)	-1.378*** (0.221)	-1.419*** (0.238)	-1.459*** (0.241)
Trips 1+ miles = [41,72)	-1.157*** (0.210)	-1.210*** (0.232)	-1.235*** (0.234)
Trips 1+ miles = [72,124)	-0.693*** (0.216)	-0.652*** (0.236)	-0.656*** (0.239)
Trips 1+ miles = [124,174)	-0.612*** (0.236)	-0.617** (0.261)	-0.669** (0.265)
Trips 1+ miles = [174,238)	-0.413 (0.272)	-0.573** (0.284)	-0.578** (0.291)
Trips 1+ miles = [238,364)	-0.456* (0.235)	-0.536** (0.255)	-0.567** (0.260)
Trips 1+ miles = 365	0 (.)	0 (.)	0 (.)
Has participated in CBC	0.0882 (0.0880)	0.150 (0.0939)	0.142 (0.0952)
Hunts birds	-0.00231 (0.158)	-0.0533 (0.173)	-0.0639 (0.174)
Gender: Female	-0.136 (0.0862)	-0.154* (0.0927)	-0.138 (0.0951)
Age: 24 years or less	0.649**	0.737**	0.628*

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Table A22 – continued from previous page

	(0.288)	(0.346)	(0.370)
Age: 25 to 34 years	0.194 (0.178)	0.216 (0.194)	0.271 (0.197)
Age: 35 to 44 years	0.279* (0.165)	0.288 (0.180)	0.304* (0.181)
Age: 55 to 64 years	-0.268** (0.127)	-0.110 (0.145)	-0.131 (0.148)
Age: 65 years and up	-0.223* (0.124)	0.109 (0.179)	0.0808 (0.182)
Education: High school	0.323 (0.250)		0.374 (0.275)
Education: Some college	0.0255 (0.137)		-0.0841 (0.152)
Education: Masters degree	0.269*** (0.101)		0.224** (0.110)
Education: Doctoral degree	0.203 (0.137)		0.0900 (0.148)
Empl. status: Part time		-0.189 (0.175)	-0.156 (0.177)
Empl. status: Looking for work		-0.978* (0.587)	-0.908 (0.590)
Empl. status: Unemployed		0.103 (0.188)	0.121 (0.191)
Empl. status: Retired		-0.308** (0.144)	-0.276* (0.147)
cut1	-2.567*** (0.227)	-2.768*** (0.238)	-2.691*** (0.254)
cut2	-1.345*** (0.218)	-1.510*** (0.227)	-1.425*** (0.244)
cut3	-0.388* (0.213)	-0.558** (0.222)	-0.476** (0.239)
Observations	807	705	690
Max. log-likelihood	-833.29	-720.01	-702.08
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

Table A23: eBird sample: Model 28-30 (of 30) to accommodate missing values

	Model 28	Model 29	Model 30
Engagement-level indicator			
Travel 1+ mile data available	0 (.)	0 (.)	0 (.)
Trips 1+ miles = 0	-2.757*** (0.204)	-2.791*** (0.208)	-2.767*** (0.224)
Trips 1+ miles = [1,4)	-2.928*** (0.237)	-3.047*** (0.244)	-3.002*** (0.262)
Trips 1+ miles = [4,7)	-2.043*** (0.246)	-2.105*** (0.251)	-1.773*** (0.281)
Trips 1+ miles = [7,10)	-1.792*** (0.335)	-2.052*** (0.349)	-1.943*** (0.356)
Trips 1+ miles = [10,21)	-1.751*** (0.226)	-1.774*** (0.229)	-1.777*** (0.247)
Trips 1+ miles = [21,41)	-1.450*** (0.235)	-1.475*** (0.240)	-1.450*** (0.257)
Trips 1+ miles = [41,72)	-1.312*** (0.224)	-1.335*** (0.227)	-1.317*** (0.251)
Trips 1+ miles = [72,124)	-0.841*** (0.230)	-0.830*** (0.233)	-0.714*** (0.255)
Trips 1+ miles = [124,174)	-0.670*** (0.253)	-0.685*** (0.258)	-0.609** (0.287)
Trips 1+ miles = [174,238)	-0.466 (0.294)	-0.467 (0.298)	-0.540* (0.316)
Trips 1+ miles = [238,364)	-0.396 (0.255)	-0.392 (0.260)	-0.418 (0.279)
Trips 1+ miles = 365	0 (.)	0 (.)	0 (.)
Has participated in CBC	0.0778 (0.0954)	0.0956 (0.0975)	0.160 (0.104)
Hunts birds	0.00672 (0.166)	-0.00191 (0.167)	-0.0502 (0.179)
Gender: Female	-0.110 (0.0936)	-0.0712 (0.0965)	-0.125 (0.104)
Age: 24 years or less	0.909***	0.893***	1.144***

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Table A23 – continued from previous page

	(0.324)	(0.334)	(0.413)
Age: 25 to 34 years	0.119 (0.188)	0.207 (0.191)	0.218 (0.212)
Age: 35 to 44 years	0.249 (0.172)	0.307* (0.174)	0.284 (0.190)
Age: 55 to 64 years	-0.267** (0.134)	-0.298** (0.137)	-0.0908 (0.156)
Age: 65 years and up	-0.170 (0.135)	-0.186 (0.137)	0.188 (0.197)
Income: Less than 25K	-0.0147 (0.200)	0.0242 (0.209)	-0.128 (0.240)
Income: 25 K to 50 K	0.113 (0.134)	0.146 (0.138)	0.135 (0.145)
Income: 75 K to 100 K	0.0129 (0.143)	0.0453 (0.145)	-0.0415 (0.156)
Income: 100 K or more	0.191 (0.121)	0.225* (0.124)	0.116 (0.134)
Education: High school		0.590** (0.281)	
Education: Some college		0.0934 (0.151)	
Education: Masters degree		0.303*** (0.111)	
Education: Doctoral degree		0.146 (0.151)	
Empl. status: Part time			-0.162 (0.187)
Empl. status: Looking for work			-0.861 (0.646)
Empl. status: Unemployed			-0.00203 (0.213)
Empl. status: Retired			-0.369** (0.160)
cut1	-2.706*** (0.240)	-2.525*** (0.255)	-2.749*** (0.272)

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Table A23 – continued from previous page

cut2	-1.457*** (0.230)	-1.252*** (0.246)	-1.424*** (0.262)
cut3	-0.488** (0.225)	-0.281 (0.241)	-0.483* (0.257)
Observations	687	673	584
Max. log-likelihood	-718.20	-696.80	-599.55
<i>t</i> in parentheses			
* $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$			

H Calculating heterogeneous population weights for eBird member survey sample

Selection-correction models allow the analyst to accommodate the possibility that there is a correlation between the *unobserved error term* in the process that leads to an individual's presence in the estimating sample and the *unobserved error term* in the process that generates the outcome variable for that individual. However, it is possible that the *observable heterogeneity* across the individuals who show up in the estimating sample could also be different from the observable heterogeneity in the general population.

In such a case, researchers often consider the use of exogenous weights. Weights are used to scale the relative frequency of people of different types in the estimating sample so that group proportions more closely match the corresponding group proportions in the population. With a fully representative estimating sample, each observation represents an equal number of people in the population as a whole, so that average preferences in the sample (for example) should be the same as average preferences in the population. If each observation in the sample represents a very different number of people in the population, then estimated average preferences are less likely to scale up to the general population.

We seek an appropriate set of weights to use when estimating our outcome equation, to explain the market extent (i.e. the maximum one-way distance a respondent is willing to travel on a day-trip to see wild birds). Many weighting schemes employ the relative frequencies of people of different types in the population divided by the relative frequencies of people of those same types in the estimating sample. The ratios of relative frequencies are then scaled so that they sum to the size of the estimating sample. Typically, the researchers bins both the population and the estimating sample according to the values of some set of exogenous variables.

For rudimentary weights, we could use the observed undifferentiated proportions of respondents at each engagement level in the two samples, (qBus, eBird) = (0.273, 0.398), (0.252, 0.275), (0.265, 0.179), and (0.210, 0.146). However, we are also concerned that engagement intensity is not fully exogenous to the maximum distance variable we seek to model. Observed proportions do not allow for the possibility of systematically different mixes of people in the two samples. Thus we adapt the conventional exogenous weighting approach to express the *fitted probabilities* of an individual from each sample exhibiting the engagement intensity that they report. We compute our weights based on the within-sample fitted probabilities that each respondent participated in eBird at each of the four possible engagement levels, where these fitted probabilities are expressed as functions of the individual's exogenous characteristics, and any error term in the fitted probabilities is implicitly discarded, making each fitted probability a function of exogenous variables only.

For our eBird data, we are concerned that (a) the relative *proportions* of respondents in our eBird sample who engage with the project at different levels might differ from (b) the corresponding proportions in the population of eBird members who turn up in a random sample from the general population (i.e. our qBus sample). We again transfer our qBus parameter estimates for the six-level ordered-probit models with the sociodemographic

characteristics of each person in our eBird member survey sample to calculate the *predicted* individual conditional engagement-level *probabilities* for respondents in our eBird member survey sample, as are shown in panel C of Figure 1 in the body of the paper. But then we also use our eBird member survey sample, *independently*, to estimate four-level ordered-probit models for engagement levels 3, 4, 5 and 6, and calculate predicted probabilities for these four engagement levels based on those parameters, where the distribution of these probabilities is shown in panel B of Figure 1 in the paper. We treat these two sets of predicted probabilities as the “expected” probabilities and the “observed” probabilities in the eBird member survey sample.

We construct our weights for each observation in the eBird sample by considering the observed engagement level for that person. We then generate a weight that reflects (a) the out-of-sample *predicted* probability that a person with these same characteristics would be at that level of engagement in the general population (qBus) sample, in ratio to (b) the within-sample *fitted* probability, estimated using the eBird member survey data, that they are at their observed level of engagement. As usual, we scale these weights so that they sum to the sample size for the eBird member survey. Figure A1 shows the smoothed density for the resulting distribution of heterogeneous weights for use in estimation of the outcome model that uses only the eBird member survey data (with a dotted line highlighting unit weights). For comparison, Figure A1 also shows what would be the four unique values of the set of homogeneous weights that would be calculated if we based the weight calculations only on the marginal distributions of engagement intensities, without reference to the heterogeneity in respondent characteristics across the qBus general population sample and the eBird member survey sample.

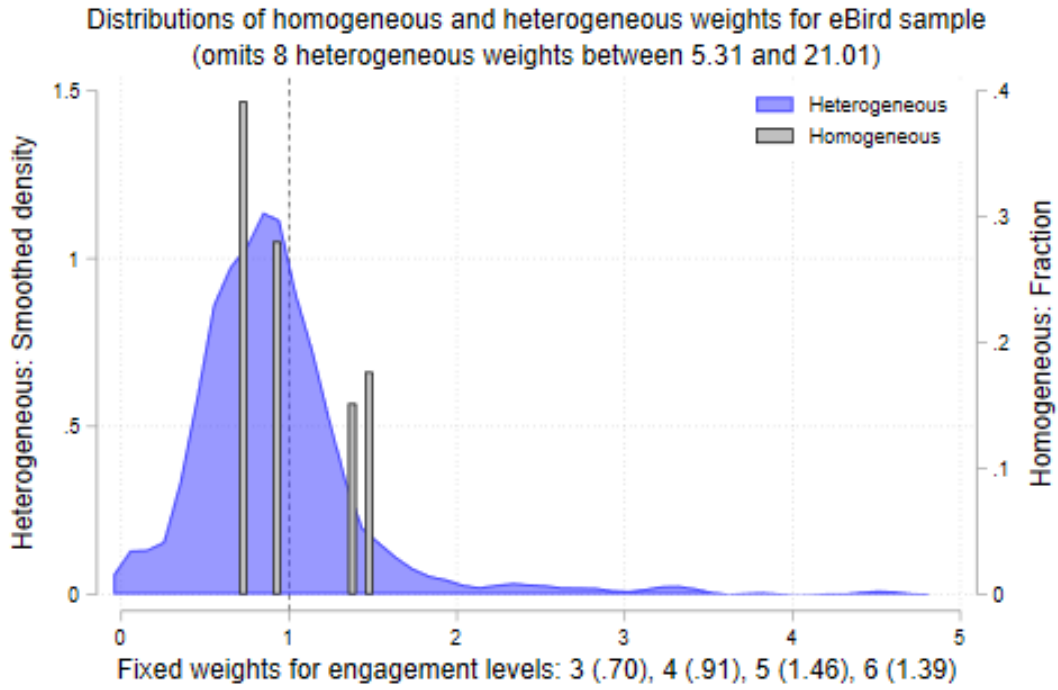


Figure A1: Distribution of weights across eBird member survey observations, where these weights serve to match engagement-intensity probabilities in the eBird member survey sample to engagement-intensity probabilities in the general-population qBus sample (six outlier weights, between 2.66 and 7.93, are not shown)

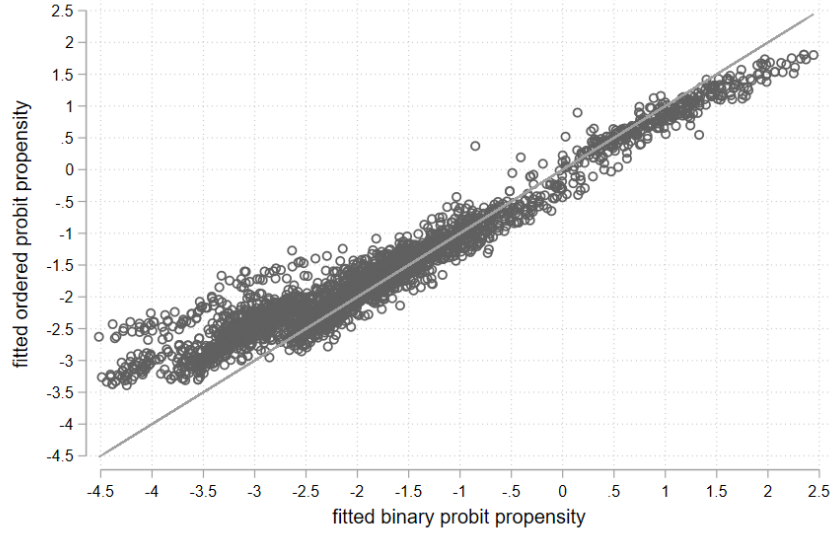


Figure A2: For 4,161 qBus general population respondents only: Fitted engagement propensities calculated from the higher-resolution ordered-probit model plotted against those from the simpler binary-probit model; equal values fall along the line

I Visualization of estimates of intermediate components

For the qBus dataset alone, which includes both members and non-members of eBird, Figure A2 shows the joint distribution of the (adjusted) fitted propensity index, $Z_i\hat{\gamma}^q$, for our new ordered-probit selection equation as well as the fitted propensity index, $Z_i\hat{\gamma}^q$ from a conventional binary-probit selection model using the same qBus data. The propensity index from our new ordered-probit selection model is somewhat higher than the index for the conventional binary model among people with low propensities to belong to eBird, but the upper part of the joint distribution coincides fairly closely. Our ordered-probit selection model recruits more information, with its multiple categories, from both non-members and members of eBird in the qBus sample, which likely accounts for the differences.

We can also consider the differences in the distributions of our two alternative IMR terms, calculated using parameter estimates from the qBus sample, *applied to individuals in our eBird member survey sample*. These two IMR variables are based on our two different selection models: (1) the binary-probit model and (2) the re-normalized (adjusted) ordered-probit model. Figure A3 shows the joint distribution of these two IMR terms.

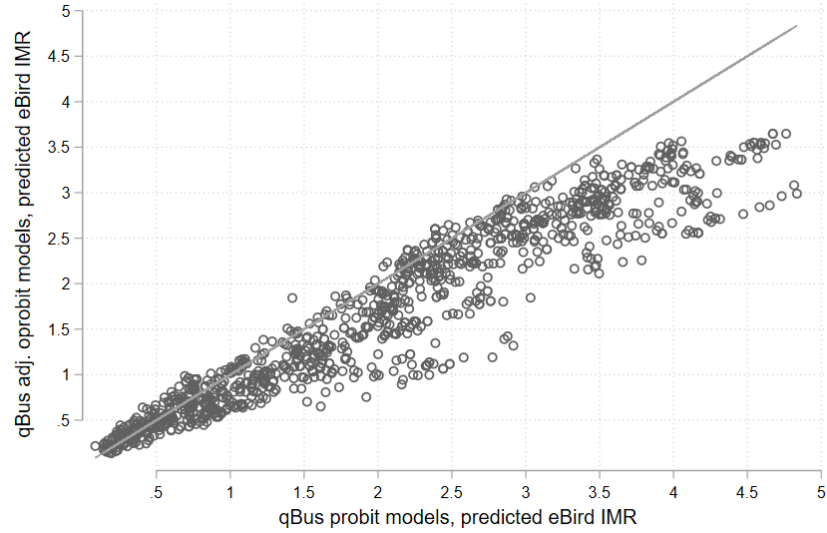


Figure A3: For 1,081 eBird member survey respondents: Predicted ordered-probit-based IMRs calculated with parameters estimated using qBus sample, plotted against predicted binary-probit-based IMRs calculated with parameters estimated using the qBus sample. For each individual observation in the eBird sample, we use the most-detailed qBus specification consistent with missing Z_j data for that observation.

Figure A4 illustrates the high degree of collinearity between the predicted inverse Mills ratio correction term and the predicted engagement propensity for the eBird sample. Had we devoted space in Table 4 to a model with only an interaction term between the demeaned engagement propensity and the intercept term in the model, the coefficient on the single additional would have adapted to the change of scale and sign in the propensity, as opposed to the inverse Mills ratio, and essentially the same values for the remaining parameters would result.

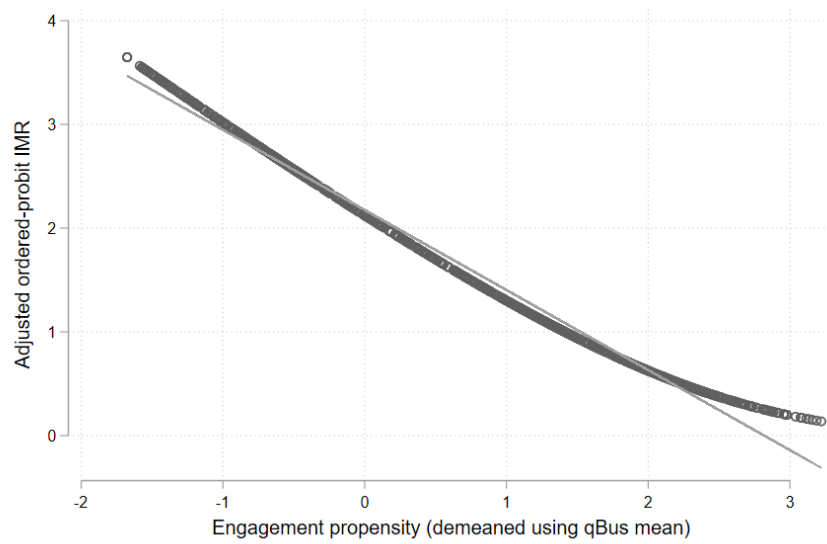


Figure A4: The relationship between our adjusted ordered-probit inverse Mills ratio term used in Model 4 in Table 4 and the underlying demeaned engagement propensity variable used to shift the basic coefficients in Model 5.

J Issues still to be addressed in the transfer of selection propensities

J.1 When the outcome equation is a conditional logit choice model, rather than a regression model

Our broader research project with the eBird sample involves destination choice models and inferred preferences for site attributes, employed to estimate non-market benefits associated with wild birds. However, Heckman selection-correction models are not appropriate when the outcome variable of interest is a discrete choice, because the latent choice propensity in a multiple discrete-choice model is *not* conditionally normally distributed.³⁷ When there is no bivariate normal error term to justify the use of a fitted IMR from a selection model as an additional regressor in an outcome equation, it is nevertheless still possible to explore the more ad hoc correction that accommodates systematic differences in selection propensities across respondents by allowing second-stage parameters to differ systematically with deviations of fitted respondent selection propensities from the average propensity in the general population. This ad hoc correction is used in Cameron and DeShazo (2013), Johnston and Abdulrahman (2017), Kolstoe and Cameron (2017) and Kolstoe et al. (2018). As mentioned in Appendix B, Terza (2009) offers models that hint at the possibility of selection-correction methods for conditional logit models, but his method would need to be adapted extensively to suit the case where the selection model is to be transferred to a different sample.

J.2 Estimated regressors and inference in a second-stage model

Of course, any two-step estimation process that does not account for the estimated property of the $\hat{\gamma}^q$ parameters embodied in the calculated IMR terms—as in Models 3 and 4 (or the fitted de-measured response propensities, as in Model 5)—can risk some bias in the inferences to be drawn in the second step. The IMR term (or fitted de-measured predicted response propensity) is an “estimated regressor” that likely overstates the amount of information in the data. It may be straightforward (if tedious), to implement an appropriate FIML estimator in the case where one does not need to contend with any missing data in the dataset to which the selection specification is to be transferred. Recall that in this case, it was necessary to estimate 30 different selection equation specifications using many combinations of none, some, or all of the categories of indicators in the full selection model.

If all variables for the selection equation were available for every observation in the CS sample having the outcome variable of interest, one could define the log-likelihood function over the full set of parameters: $\gamma, \beta, \sigma_\eta, \sigma_\epsilon, \rho$. The structure of the two-step model could be preserved, but the two equations could be estimated simultaneously, constraining the γ parameters to be the same in both the selection equation (using the qBus sample) and the

³⁷Some researchers (e.g. Yuan et al. (2015)) have inserted a fitted inverse Mills ratio (IMR) into a second-stage discrete-choice model, although there seems to be no statistical justification for this particular transformation of the fitted selection propensity.

outcome equation (using the IMR term), where the index for the IMR variable is constructed using the γ parameters combined with the Z_j variables for the eBird dataset. The matter of how to construct the weights would need to be resolved, of course. We do not attempt this FIML estimation here, because of the significant amount of missing data for the selection equation applied to the eBird sample, and corresponding proliferation of different specifications necessary to provide predicted propensities, IMRs, and weights that maximize our use of the available data for each eBird respondent. While joint estimation of 30 different ordered-probit equations plus the outcome equations would likely be possible, we would not expect it to make any qualitative difference in our findings.

J.3 Other possible layers of selection

Our estimating sample for the illustrative market-extent model in this paper consists of respondents to our eBird member survey who provided complete data for all except the (typically sensitive) detailed income variable. The selection-correction strategies we feature in this paper presume that this group of eBird member survey respondents is representative of eBird members, an assumption we make to permit us to focus on the problem of systematic selection into eBird engagement at different levels of intensity.

Of course, there may be a variety of reasons why invited eBird members decide not to participate in our survey. In other research, we have sought to control for heterogeneous selection across all eBird members (rather than the general population) by linking the center of gravity of their birding trips to a specific census tract, which we impute to be their home census tract. We have employed census tract attributes as proxies for possible systematic variation across birder characteristics because there is no sociodemographic information available for eBird members who did not respond to our survey. We then employ these various census tract attributes to construct a “propensity of an invited eBird member to respond to our survey” and use this propensity in an attempt to control crudely for selection into our estimating sample for destination choice models. We do not attempt to overlay that correction procedure in addition to the strategies employed here. It is possible that the selection of eBird members into our survey, based on the attributes of their home zipcode relative to those of the general population, is dominated by the selection of the general population into eBird participation, but this is an empirical question that is beyond the scope of this study.

Even with the illustrative example concerning the extent of the market for birding excursions, it is possible that sample selection may occur along more than one dimension. Respondents to our eBird survey may have unobserved characteristics that make them simultaneously more likely (than otherwise expected) to be members of eBird and also more likely than average to participate in travel of more than one mile from home to observe birds. In other research, it is this second behavior upon which we base our models of the “active” recreational use of opportunities to watch wild birds. In addition to the eBird engagement-level variable captured by our ordinal variable $CS6_i$, we can also distinguish between birders who do, or do not, travel more than one mile to see birds, in both the qBus sample and the eBird sample. Three categories of actual bird-watching might be distinguished: no birding trips, trips only less than 1 mile, and trips of one mile or more. Thus the ordinal eBird

engagement levels might be supplemented by a second (presumably correlated) ordinal variable that captures heterogeneity in the actual bird-watching behavior of respondents in both surveys. Models with selection on two (correlated) latent variables would require working with trivariate normal joint distributions of the error terms. These models are also beyond the scope of the current paper, again because of the 30 different ordered-probit selection equations necessary to accommodate transfer of our selection model from the qBus sample to the eBird member survey sample with its missing values for different variables.

References

- Badura, T., S. Ferrini, M. Burton, A. Binner, and I. J. Bateman (2020). Using individualised choice maps to capture the spatial dimensions of value within choice experiments. *Environmental Resource Economics* 75(2), 297–322.
- Bakhtiari, F., J. B. Jacobsen, B. J. Thorsen, T. H. Lundhede, N. Strange, and M. Boman (2018). Disentangling distance and country effects on the value of conservation across national borders. *Ecological Economics* 147, 11–20.
- Bateman, I. J., B. H. Day, S. Georgiou, and I. Lake (2006). The aggregation of environmental benefit values: Welfare measures, distance decay and total wtp. *Ecological Economics* 60(2), 450–460.
- Cameron, T. A. and J. DeShazo (2013). Demand for health risk reductions. *Journal of Environmental Economics and Management* 65(1), 87–109.
- Cameron, T. A. and J. Englin (1997). Respondent experience and contingent valuation of environmental goods. *Journal of Environmental Economics and Management* 33(3), 296–313.
- De Valck, J. and J. Rolfe (2017). Spatial heterogeneity in stated preference valuation: Status, challenges and road ahead. *International Review of Environmental and Resource Economics* 11(4), 355–422.
- Dundas, S. J. and R. H. von Haefen (2020). The effects of weather on recreational fishing demand and adaptation: Implications for a changing climate. *Journal of the Association of Environmental and Resource Economists* 7(2), 209–242.
- Greene, W. H. (2012). *Econometric Analysis (7 th)*. Upper Saddle River, NJ: Prentice Hall.
- Heckman, J. J. (1979). Sample selection bias as a specification error. *Econometrica: Journal of the econometric society*, 153–161.
- Holland, B. M. and R. J. Johnston (2017). Optimized quantity-within-distance models of spatial welfare heterogeneity. *Journal of Environmental Economics and Management* 85, 110–129.
- Jank, W. and P. K. Kannan (2005). Understanding geographical markets of online firms using spatial models of customer choice. *Marketing Science* 24(4), 623–634.
- Johnston, R. J. and A. S. Abdulrahman (2017). Systematic non-response in discrete choice experiments: implications for the valuation of climate risk reductions. *Journal of Environmental Economics and Policy* 6(3), 246–267.
- Johnston, R. J., E. Y. Besedin, and B. M. Holland (2019). Modeling distance decay within valuation meta-analysis. *Environmental Resource Economics* 72(3), 657–690.

- Keeler, B. L., S. A. Wood, S. Polasky, C. Kling, C. T. Filstrup, and J. A. Downing (2015). Recreational demand for clean water: evidence from geotagged photographs by visitors to lakes. *Frontiers in Ecology and the Environment* 13(2), 76–81.
- Kolstoe, S. and T. A. Cameron (2017). The Non-market Value of Birding Sites and the Marginal Value of Additional Species: Biodiversity in a Random Utility Model of Site Choice by eBird Members. *Ecological Economics* 137, 1–12.
- Kolstoe, S., T. A. Cameron, and C. Wilsey (2018). Climate, land cover, and bird populations: Differential impacts on the future welfare of birders across the pacific northwest. *Agricultural and Resource Economics Review* 47(2), 272–310.
- Logar, I. and R. Brouwer (2018). Substitution effects and spatial preference heterogeneity in single- and multiple-site choice experiments. *Land Economics* 94(2), 302–322.
- Loomis, J. B. (1996). How large is the extent of the market for public goods: evidence from a nationwide contingent valuation survey. *Applied economics* 28(7), 779–782.
- Newbold, S., R. D. Simpson, D. M. Massey, M. T. Heberling, W. Wheeler, J. Corona, and J. Hewitt (2018). Benefit transfer challenges: Perspectives from us practitioners. *Environmental Resource Economics* 69(3), 467–481.
- Olsen, R. J. (1980). A least-squares correction for selectivity bias. *Econometrica* 48(7), 1815–1820.
- Roberts, A. J., P. K. Devers, S. Knoche, P. I. Padding, and R. Raftovich (2017). Site preferences and participation of waterbird recreationists: Using choice modelling to inform habitat management. *Journal of Outdoor Recreation and Tourism-Research Planning and Management* 20, 52–59.
- Rodrigue, J.-P., C. Comtois, and B. Slack (2016). *The geography of transport systems*. Routledge.
- Rosenberg, K. V., A. M. Dokter, P. J. Blancher, J. R. Sauer, A. C. Smith, P. A. Smith, J. C. Stanton, A. Panjabi, L. Helft, M. Parr, and P. P. Marra (2019). Decline of the north american avifauna. *Science*.
- Sessions, C., S. A. Wood, S. Rabotyagov, and D. M. Fisher (2016). Measuring recreational visitation at us national parks with crowd sourced photographs. *Journal of Environmental Management* 183, 703–711.
- Smith, V. K. (1993). Nonmarket valuation of environmental resources: An interpretive appraisal. *Land Economics* 69(1), 1–26.
- Sonter, L. J., K. B. Watson, S. A. Wood, and T. H. Ricketts (2016). Spatial and temporal dynamics and value of nature-based recreation, estimated via social media. *PLoS one* 11(9), e0162372.

- Swait, J., C. Franceschinis, and M. Thiene (2020). Antecedent volition and spatial effects: Can multiple goal pursuit mitigate distance decay? *Environmental Resource Economics* 75(2), 243–270.
- Terza, J. V. (1998). Estimating count data models with endogenous switching: Sample selection and endogenous treatment effects. *Journal of Econometrics* 84(1), 129–154.
- Terza, J. V. (2009). Parametric nonlinear regression with endogenous switching. *Econometric Reviews* 28(6), 555–580.
- Vella, F. (1998). Estimating models with sample selection bias: a survey. *Journal of Human Resources*, 127–169.
- Vogdrup-Schmidt, M., A. L. Abatayo, J. F. Shogren, N. Strange, and B. J. Thorsen (2019). Factors affecting support for transnational conservation targeting migratory species. *Ecological Economics* 157, 156–164.
- von Haefen, R. H. (2008). Latent consideration sets and continuous demand systems. *Environmental Resource Economics* 41(3), 363–379.
- Walsh, P. J., J. W. Milon, and D. O. Scrogin (2011). The spatial extent of water quality benefits in urban housing markets. *Land Economics* 87(4), 628–644.
- Wood, S. A., A. D. Guerry, J. M. Silver, and M. Lacayo (2013). Using social media to quantify nature-based tourism and recreation. *Scientific reports* 3, srep02976.
- Wooldridge, J. M. (2002). *Econometric Analysis of Cross Section and Panel Data*. MIT Press.-2002.
- Yuan, Y., K. J. Boyle, and W. You (2015). Sample selection, individual heterogeneity, and regional heterogeneity in valuing farmland conservation easements. *Land Economics* 91(4), 627–649.